Introduction to XFST

- XFST is an interface giving access to finite-state operations (algorithms such as union, concatenation, iteration, intersection, composition etc.)
- XFST includes a regular expression compiler
- The interface of XFST includes a lookup operation (apply up) and a generation operation (apply down)
- The regular expression language employed by XFST is an extended version of standard regular expressions

\{cat\}    equivalent to \([c\ a\ t]\)
\[\]\     the empty string
0         the empty string
[A]       bracketing; equivalent to A
A\|B      union
(A)       optionality; equivalent to \([A]0\]
A&B       intersection
A\ B      concatenation
A\-B      set difference

\textbf{Introduction to XFST}

a        a simple symbol
c a t    a concatenation of three symbols
\[c a t\] grouping brackets
?        denotes any single symbol
\%+      the literal plus-sign symbol
\%*      the literal asterisk symbol (and similarly for \%, \%, \% etc.)
\+\text{\texttt{Noun}} single symbol with multicharacter print name
\%+\text{\texttt{Noun}} single symbol with multicharacter print name
cat      a single multicharacter symbol

\textbf{Introduction to XFST}

A*       Kleene-star
A+       one or more iterations
?*       the universal language
~A       the complement of A; equivalent to \([?* - A]\)
~[?*]    the empty language
**Introduction to XFST — denoting relations**

A .x. B  Cartesian product; relates every string in A to every string in B
a:b  shorthand for [a .x. b]
%+P1:s  shorthand for [%+P1 .x. s]
%+Past:ed  shorthand for [%+Past .x. ed]
%+Prog:ing  shorthand for [%+Prog .x. ing]

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**Introduction to XFST — useful abbreviations**

$\text{A}$ the language of all the strings that contain A; equivalent to [?* A ?*]

A/B the language of all the strings in A, ignoring any strings from B, e.g.,
a*/b includes strings such as a, aa, aaa, ba, ab, aba etc.
\A any single symbol, minus strings in A. Equivalent to [? - A], e.g.,
\b any single symbol, except 'b'. Compare to:
\sim A the complement of A, i.e., [?* - A]

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**Introduction to XFST — user interface**

prompt% H:\class\data\shuly\xfst

xfst> help
xfst> help union net
xfst> exit
xfst> read regex [dog | cat];
xfst> read regex <myfile.regex
xfst> apply up dog
xfst> apply down dog
xfst> pop stack
xfst> clear stack
xfst> save stack myfile.fsm

---

**Introduction to XFST — example**

[[leave %VBZ .x. leaves] | [leave %VB .x. leave] | [leave %VBG .x. leaving] | [leave %VBD .x. left] | [leave %NN .x. leave] | [leave %NNS .x. leaves] | [left %JJ .x. left] ]
Introduction to XFST – example of lookup and generation

APPLY DOWN> leave+VBD
left
APPLY UP> leaves
leave+NNS
leave+VBZ
leaf+NNS

Introduction to XFST – variables

xfst> define Myvar;
xfst> define Myvar2 [d o g | c a t];
xfst> undefined Myvar;

xfst> define var1 [b i r d | f r o g | d o g];
xfst> define var2 [d o g | c a t];
xfst> define var3 var1 | var2;
xfst> define var4 var1 var2;
xfst> define var5 var1 & var2;
xfst> define var6 var1 - var2;

Introduction to XFST – replace rules

Replace rules are an extremely powerful extension of the regular expression metalanguage.

The simplest replace rule is of the form

\[ \text{upper} \rightarrow \text{lower} \parallel \text{leftcontext} \_ \text{rightcontext} \]

Its denotation is the relation which maps string to themselves, with the exception that an occurrence of \textit{upper} in the input string, preceded by \textit{leftcontext} and followed by \textit{rightcontext}, is replaced in the output by \textit{lower}. 
Introduction to XFST – replace rules

Word boundaries can be explicitly referred to:

```
xfst> define Vowel [a|e|i|o|u];
xfst> e -> ' || [.##] [c | d | l | s] _ [Vowel];
```

Introduction to XFST – replace rules

Contexts can be omitted:

```
xfst> define Rule1 N -> m || _ p ;
xfst> define Rule2 N -> n ;
xfst> define Rule3 p -> m || m _ ;
```

This can be used to clear unnecessary symbols introduced for "bookkeeping":

```
xfst> define Rule1 % MorphemeBoundary -> 0;
```

Introduction to XFST – replace rules

The language Bambona has an underspecified nasal morpheme N that is realized as a labial m or as a dental n depending on its environment: N is realized as m before p and as n elsewhere.

The language also has an assimilation rule which changes p to m when the p is followed by m.

```
xfst> clear stack ;
xfst> define Rule1 N -> m || _ p ;
xfst> define Rule2 N -> n ;
xfst> define Rule3 p -> m || m _ ;
xfst> read regex Rule1 .o. Rule2 .o. Rule3 ;
```

Introduction to XFST – replace rules

Rules can define multiple replacements:

```
[ A -> B, B -> A ]
```

or multiple replacements that share the same context:

```
[ A -> B, B -> A || L _ R ]
```

or multiple contexts:

```
[ A -> B || L1 _ R1, L2 _ R2 ]
```

or multiple replacements and multiple contexts:

```
[ A -> B, B -> A || L1 _ R1, L2 _ R2 ]
```
Introduction to XFST – replace rules

Rules can apply in parallel:

xfst> clear stack
xfst> read regex a -> b .o. b -> a ;
xfst> apply down abba
aaaa
xfst> clear stack
xfst> read regex b -> a .o. a -> b ;
xfst> apply down abba
bbbb
xfst> clear stack
xfst> read regex a -> b , b -> a ;
xfst> apply down abba
baab

Introduction to XFST – morphology

English verb morphology:

define Vowel [a|e|i|o|u] ;
define Cons [? = Vowel] ;
define base [(dip) | (print) | (tuss) | (toss) | (bake) | (move)] ;
define suffix [0 | (s) | (ed) | (ing)] ;
define form [base %+ suffix] ;
define FinalS [s %+ s] -> [s %+ e s] ;
define FinalE e -> 0 || _ %+ [e | i] ;
define DoubleFinal b -> [b b], d -> [d d], f -> [f f],
    g -> [g g], k -> [k k], l -> [l l], m -> [m m],
    n -> [n n], p -> [p p], r -> [r r], s -> [s s],
    t -> [t t], z -> [z z] || Cons Vowel %+ Vowel ;
define RemovePlus %+ -> 0 ;
read regex form .o. DoubleFinal .o. FinalS .o. FinalE
    .o. RemovePlus ;

Introduction to XFST – replace rules

When rules that have contexts apply in parallel, the rule separator
is a double comma:

xfst> clear stack
xfst> read regex
b -> a || .# .s ?* _ , a -> b || _ ?* e .# ;
xfst> apply down sabbue
sbaabe

Introduction to XFST – morphology

English spell checking:

clear ;
define A [i e] -> [e i] || c _ , ,
    [e i] -> [i e] || [? = c] _ ;
define B [[e i] -> [i e]] .o.
    [[i e] -> [e i] || c _];
read regex B ;
Introduction to XFST – morphology

Hebrew adjective inflection:

clear stack;
define base [{gdwL} | {yph} | {xbrwty} | {rk} | {adm} | {q$h} | {ap$ry}];
define suffix [0 | {hm} | {ym} | {wt}] ;
define form [base %- suffix];
define FinalH h -> 0 || _ %+ ? ;
define FinalY y -> t || y %+ _ ;
define RemovePlus %+ -> 0 ;
read regex form .o. FinalH .o. FinalY .o. RemovePlus;

Introduction to XFST – marking

The special symbol "..." in the right-hand side of a replace rule stands for whatever was matched in the left-hand side of the rule.

xfst> clear stack;
xfst> read regex [a|e|i|o|u] -> %[ ... %];
xfst> apply down unnecessarily
[u]nn[e|c][e]ss[a]r[i]ly

Introduction to XFST – shallow parsing

Assume that text is represented as strings of part-of-speech tags, using 'd' for determiner, 'a' for adjective, 'n' for noun, and 'v' verb, etc. In other words, in this example the regular expression symbols represent whole words rather than single letters in a text.

Assume that a noun phrase consists of an optional determiner, any number of adjectives, and one or more nouns:

[(d) a* n*]

This expression denotes an infinite set of strings, such as "n" (cats), "aan" (discriminating aristocratic cats), "nn" (cat food), "dn" (many cats), "dann" (that expensive cat food) etc.
Introduction to XFST – shallow parsing

A simple noun phrase parser can be thought of as a transducer that inserts markers, say, a pair of braces \{ \}, around noun phrases in a text. The task is not as trivial as it seems at first glance. Consider the expression

\[
[(d) \ a^* \ n^+ \rightarrow \%(...\%)]
\]

Applied to the input “danvn” (many small cats like milk) this transducer yields three alternative bracketings:

```
xfst> apply down danvn
da{n}{v{n}}
d{an}{v{n}}
{dan}{v{n}}
```

Introduction to XFST – the coke machine

A vending machine dispenses drinks for 65 cents a can. It accepts any sequence of the following coins: 5 cents (represented as ‘n’), 10 cents (‘d’) or 25 cents (‘q’). Construct a regular expression that compiles into a finite-state automaton that implements the behavior of the soft drink machine, pairing “PLONK” with a legal sequence that amounts to 65 cents.

Introduction to XFST – longest match

For certain applications it may be desirable to produce a unique parse, marking the maximal expansion of each NP: “\{(dan}\{v\{n\}\}”. Using the left-to-right, longest-match replace operator \(\rightarrow\) instead of the simple replace operator \(\rightarrow\) yields the desired result:

\[
[(d) \ a^* \ n^+ \rightarrow \%(...\%)]
\]

```
xfst> apply down danvn
{dan}{v{n}}
```

Introduction to XFST – the coke machine

The construction \(A^n\) denotes the concatenation of \(A\) with itself \(n\) times.

Thus the expression \([n . x . c^5]\) expresses the fact that a nickel is worth 5 cents.

A mapping from all possible sequences of the three symbols to the corresponding value:

\[
[[n \ . x . c^5] \ | \ [d . x . c^10] \ | \ [q . x . c^25]]^*
\]

The solution:

```
[[n . x . c^5] | [d . x . c^10] | [q . x . c^25]]^*
 .?
[c^65 . x . PLONK]
```
clear stack
define SixtyFiveCents
[[n .x. c^5] | [d .x. c^-10] | [q .x. c^-25]]* ;
define BuyCoke
SixtyFiveCents .o. [c^-65 .x. PLONK] ;

---

The next refinement is to ensure that as much money as possible is converted into soft drinks and to remove any ambiguity in how the extra change is to be reimbursed.

clear stack
define SixtyFiveCents
[[n .x. c^5] | [d .x. c^-10] | [q .x. c^-25]]* ;
define ReturnChange SixtyFiveCents .o.
[c^-65 .x. PLONK]* [c^-25 .x. q]*
[c^-10 .x. d]* [c^-5 .x. n]* ;
define ExactChange ReturnChange .o.
["*[q q q | [q q | d] d [d | n] | n n]] ;

---

In order to ensure that extra money is paid back, we need to modify the lower language of BuyCoke to make it a subset of [PLONK* q* d* n*].

To ensure that the extra change is paid out only once, we need to make sure that quarters get paid before dimes and dimes before nickels.

clear stack
define SixtyFiveCents
[[n .x. c^5] | [d .x. c^-10] | [q .x. c^-25]]* ;
define ReturnChange SixtyFiveCents .o.
[c^-65 .x. PLONK]* [c^-25 .x. q]*
[c^-10 .x. d]* [c^-5 .x. n]* ;

define IgnoreGarbage
[[ ExactChange ]]/[
[q | d | n]] ;
Applications of finite-state technology in NLP

- Phonology; language models for speech recognition
- Representing lexicons and dictionaries
- Morphology; morphological analysis and generation
- Shallow parsing
- Named entity recognition
- Sentence boundary detection; segmentation
- Translation...