Parsing

Recognition: Given a (context-free) grammar G and a string of words w, determine whether $w \in L(G)$.

Parsing: If $w \in L(G)$, produce the (tree) structure that is assigned by G to w.

Computational Linguistics

Parsing

Parameters that define different parsing algorithms:

Orientation: Top-down vs. bottom-up vs. mixed

Direction: Left-to-right vs. right-to-left vs. mixed (e.g., island-driven)

Handling multiple choice: Dynamic programming vs. parallel processing vs. backtracking

Search: Breadth-first or Depth-first

Computational Linguistics

204

206

Parsing

General requirements for a parsing algorithm:

- Generality: the algorithm must be applicable to any grammar
- Completeness: the algorithm must produce *all* the results in case of ambiguity
- Efficiency
- Flexibility: a good algorithm can be easily modified

Computational Linguistics

207

205

An example grammar

 $\begin{array}{lll} D \rightarrow \textit{the} & & \textit{NP} \rightarrow \textit{D} \; \textit{N} \\ \textit{N} \rightarrow \textit{cat} & & \textit{PP} \rightarrow \textit{P} \; \textit{NP} \\ \textit{N} \rightarrow \textit{hat} & & \textit{NP} \rightarrow \textit{NP} \; \textit{PP} \\ \hline \end{array}$

 $P \rightarrow in$

Example sentences:

the cat in the hat

the cat in the hat in the hat

A bottom-up recognition algorithm

Assumptions:

- The grammar is given in Chomsky Normal Form: each rule is either of the form $A \to B$ C (where A, B, C are non-terminals) or of the form $A \to a$ (where a is a terminal).
- The string to recognize is $w = w_1 \cdots w_n$.
- A set of indices $\{0,1,\ldots,n\}$ is defined to point to positions between the input string's words:

```
0 the 1 cat 2 in 3 the 4 hat 5
```

Computational Linguistics

The CYK algorithm

```
for j := 1 to n do

for all rules A \to w_j do

chart[j-1,j] := chart[j-1,j] \cup \{A\}

for i := j-2 downto 0 do

for k := i+1 to j-1 do

for all B \in chart[i,k] do

for all C \in chart[k,j] do

for all rules A \to B C do

chart[i,j] := chart[i,j] \cup \{A\}

if S \in chart[0,n] then accept else reject
```

Computational Linguistics

The CYK algorithm

Bottom-up, chart-based recognition algorithm for grammars in CNF

To recognize a string of length n, uses a *chart*: a bi-dimensional matrix of size $n \times (n+1)$

Invariant: a non-terminal A is stored in the [i,j] entry of the chart iff $A \Rightarrow w_{i+1} \cdots w_j$

Consequently, the chart is triangular. A word w is recognized iff the start symbol S is in the [0,n] entry of the chart

The idea: build all constituents up to the i-th position before constructing the i+1 position; build smaller constituents before constructing larger ones

Computational Linguistics

The CYK algorithm

Extensions:

210

- Parsing in addition to recognition
- Support for ϵ -rules
- General context-free grammars (not just CNF)

211

209

Parsing schemata

To provide a unified framework for discussing various parsing algorithms we use *parsing schemata*, which are generalized schemes for describing the principles behind specific parsing algorithms. This is a generalization of the *parsing as deduction* paradigm.

A parsing schema consists of four components:

- a set of items
- a set of axioms
- a set of deduction rules
- a set of goal items

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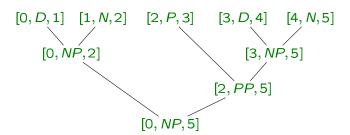
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212

CYK parsing schema: deduction example

D
ightarrow the NP
ightarrow DN N
ightarrow cat PP
ightarrow PNP NP NP PP
ightarrow in

0 the 1 cat 2 in 3 the 4 hat 5



Parsing schema: CYK

Given a grammar $G = \langle \Sigma, V, S, P \rangle$ and a string $w = w_1 \cdots w_n$:

Items: [i,A,j] for $A \in V$ and $0 \le i,j \le n$ (state that $A \stackrel{*}{\Rightarrow} w_{i+1} \cdots w_j$)

Axioms: [i, A, i+1] when $A \rightarrow w_{i+1} \in P$

Goals: [0, S, n]

Inference rules:

$$\frac{[i,B,j] \quad [j,C,k]}{[i,A,k]} \quad A \to B \ C$$

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Parsing: bottom-up schema (Shift-Reduce)

Items: $[\alpha \bullet, j]$ (state that $\alpha w_{j+1} \cdots w_n \stackrel{*}{\Rightarrow} w_1 \cdots w_n$)

Axioms: [•, 0]

Goals: $[S \bullet, n]$

Inference rules:

Shift
$$\frac{[\alpha \bullet,j]}{[\alpha w_{j+1} \bullet,j+1]}$$
 Reduce
$$\frac{[\alpha \gamma \bullet,j]}{[\alpha B \bullet,i]} \quad B \to \gamma$$

Bottom-up deduction: example

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Parsing: top-down schema

217

219

Item form: $[\bullet \beta, j]$ (state that $S \stackrel{*}{\Rightarrow} w_1 \cdots w_j \beta$)

Axioms: $[\bullet S, 0]$

Goals: $[\bullet, n]$

218

Inference rules:

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Scan
$$rac{[ullet w_{j+1}eta,j]}{[ulleteta,j+1]}$$

Predict
$$\frac{[\bullet B\beta,j]}{[\bullet \gamma\beta,j]} \quad B \to \gamma$$

Computational Linguistics

Top-down deduction: example

Input: 0 the 1 cat 2 in 3 the 4 hat 5

 $[\bullet NP, 0]$ axiom predict $NP \rightarrow NP PP$ [•*NP PP*, 0] $[\bullet D \ N \ PP, 0]$ predict $NP \rightarrow D N$ [•the N PP,0] predict $D \rightarrow the$ [•*N PP*, 1] scan [•cat PP, 1] predict $N \rightarrow cat$ $[\bullet PP, 2]$ scan $[\bullet P NP, 2]$ predict $PP \rightarrow P NP$ predict $P \rightarrow in$ [•in NP, 2] $[\bullet NP, 3]$ scan

 $[\bullet NP, 3] \qquad \text{scan}$ $[\bullet D N, 3] \qquad \text{predict } NP \to D N$

[•,5] scan

Top-down parsing: algorithm

```
Parse(\beta,j)::

if \beta = w_{j+1} \cdot \beta' then return parse(\beta',j+1)
else if \beta = B \cdot \beta' then

for every rule B \to \gamma \in P

if Parse(\gamma \cdot \beta',j) then return true
return false

if Parse(S,0) then accept else reject
```

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An example grammar

 $S \rightarrow NP VP$ $Det \rightarrow that | this | a$ $S \rightarrow Aux NP VP$ Noun \rightarrow book |flight | meal $S \rightarrow VP$ Verb → book | include | includes VP → Verb $Prep \rightarrow from \mid to \mid on$ Proper-Noun → Houston | TWA VP → Verb NP $NP \rightarrow Det Nominal$ $Aux \rightarrow does$ *NP* → *Proper-Noun* Nominal → Noun Nominal → Noun Nominal Nominal → Nominal PP $PP \rightarrow Prep NP$

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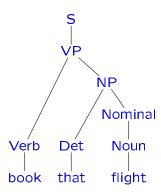
Top-down vs. Bottom-up parsing

Two inherent constraints:

- 1. The root of the tree is S
- 2. The yield of the tree is the input word

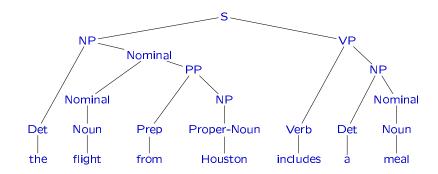
Computational Linguistics 22

An example derivation tree



Computational Linguistics 224 Computational Linguistics 225

An example derivation tree

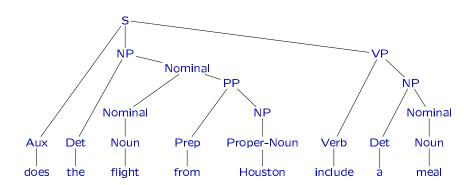


Computational Linguistics 226

Top-down vs. Bottom-up parsing

When expanding the top-down search space, which local trees are created?

An example derivation tree



Computational Linguistics

Top-down vs. Bottom-up parsing

To reduce "blind" search, add bottom-up filtering.

Observation: when trying to $Parse(\beta,j)$, where $\beta=B\gamma$, the parser succeeds only if $B\stackrel{*}{\Rightarrow} w_{j+1}\beta$.

Definition: A word w is a **left-corner** of a non-terminal B iff $B \stackrel{*}{\Rightarrow} w\beta$ for some β .

Top-down parsing with bottom-up filtering

```
\begin{aligned} &\operatorname{Parse}(\beta,\mathbf{j}) \ :: \\ &\operatorname{if} \ \beta = w_{j+1} \cdot \beta' \ \operatorname{then} \ \operatorname{return} \ \operatorname{parse}(\beta',j+1) \\ &\operatorname{else} \ \operatorname{if} \ \beta = B \cdot \beta' \ \operatorname{then} \end{aligned} \\ &\underbrace{ \  \  \, \operatorname{if} \ w_{j+1} \ \operatorname{is} \ \operatorname{a} \ \operatorname{left-corner} \ \operatorname{of} \ B \ \operatorname{then} }_{ \  \  \, \operatorname{for} \ \operatorname{every} \ \operatorname{rule} \ B \ \to \ \gamma \in P }_{ \  \  \, \operatorname{if} \ \operatorname{Parse}(\gamma \cdot \beta',j) \ \operatorname{then} \ \operatorname{return} \ \operatorname{true} } \end{aligned}
```

if Parse(S,0) then accept else reject

Computational Linguistics

Top-down parsing: repeated generation of sub-trees



Computational Linguistics

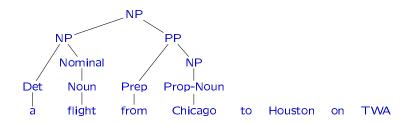
Top-down vs. Bottom-up parsing

Even with bottom-up filtering, top-down parsing suffers from the following problems:

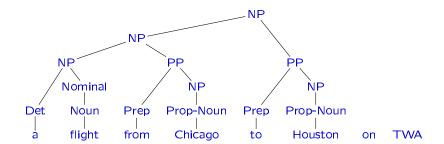
- Left recursive rules can cause non-termination: $NP \rightarrow NP PP$.
- Even when parsing terminates, it might take exponentially many steps.
- Constituents are computed over and over again

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Top-down parsing: repeated generation of sub-trees



Top-down parsing: repeated generation of sub-trees



Computational Linguistics

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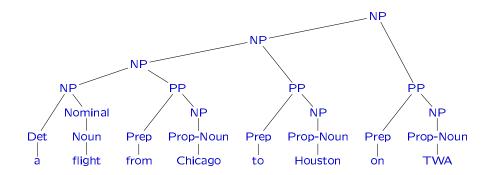
Top-down parsing: repeated generation of sub-trees

Reduplication:

Constituent	#
a flight	4
from Chicago	3
to Houston	2
on TWA	1
a flight from Chicago	3
a flight from Chicago to Houston	2
a flight from Chicago to Houston on TWA	1

Computational Linguistics

Top-down parsing: repeated generation of sub-trees



Computational Linguistics

235

Top-down vs. Bottom-up parsing

When expanding the bottom-up search space, which local trees are created?

Top-down vs. Bottom-up parsing

Bottom-up parsing suffers from the following problems:

- All possible analyses of every substring are generated, even when they can never lead to an S, or can never combine with their neighbors
- ϵ -rules can cause performance degradation
- Reduplication of effort

Computational Linguistics

- 4

Earley's parsing algorithm

Basic concepts:

Dotted rules: if $A \to \alpha\beta$ is a grammar rule then $A \to \alpha \bullet \beta$ is a dotted rule.

Edges: if $A \to \alpha \bullet \beta$ is a dotted rule and i, j are indices into the input string then $[i, A \to \alpha \bullet \beta, j]$ is an edge. An edge is **passive** (or **complete**) if $\beta = \epsilon$, **active** otherwise.

Actions: The algorithm performs three operations: *scan*, *predict* and *complete*.

Computational Linguistics

Earley's parsing algorithm

• Dynamic programming: partial results are stored in a chart

• Combines top-down predictions with bottom-up scanning

• No reduplication of computation

• Left-recursion is correctly handled

• ϵ -rules are handled correctly

• Worst-case complexity: $O(n^3)$

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239

Earley's parsing algorithm

scan: read an input word and add a corresponding complete edge to the chart.

predict: when an active edge is added to the chart, predict all possible edges that can follow it

complete: when a complete edge is added to the chart, combine it with appropriate active edges

Earley's parsing algorithm

rightsisters: given an active edge $A \rightarrow \alpha \bullet B\beta$, return all dotted rules $B \rightarrow \bullet \gamma$

leftsisters: given a complete edge $B \to \gamma \bullet$, return all dotted edges $A \rightarrow \alpha \bullet B\beta$

combination:

$$[i, A \rightarrow \alpha \bullet B\beta, k] * [k, B \rightarrow \gamma \bullet, j] = [i, A \rightarrow \alpha B \bullet \beta, j]$$

Computational Linguistics

Parsing: Earley deduction

Inference rules:

Computational Linguistics

Parsing: Earley deduction

Item form: $[i, A \rightarrow \alpha \bullet \beta, j]$ (state that $S \stackrel{*}{\Rightarrow} w_1 \cdots w_i A_{\gamma}$, and also that $\alpha \stackrel{*}{\Rightarrow} w_{i+1} \cdots w_i$)

Axioms: $[0,S' \rightarrow \bullet S,0]$

Goals: $[0,S' \rightarrow S \bullet, n]$

Computational Linguistics

Earley's parsing algorithm

```
Parse ::
    enteredge([0,S' \rightarrow \bullet S,0])
    for j := 1 to n do
      for every rule A \rightarrow w_i do
         enteredge([j-1,A \rightarrow w_i \bullet,j])
```

if $S' \rightarrow S \bullet \in C[0,n]$ then accept else reject

Earley's parsing algorithm

```
enteredge(i,edge,j) ::
   if edge ∉ C[i,j] then /* occurs check */
    C[i,j] := C[i,j] ∪ {edge}
   if edge is active then /* predict */
     for edge' ∈ rightsisters(edge) do
        enteredge([j,edge',j])
   if edge is passive then /* complete */
     for edge' ∈ leftsisters(edge) do
        for k such that edge' ∈ C[k,i] do
        enteredge([k,edge'*edge,j])
```