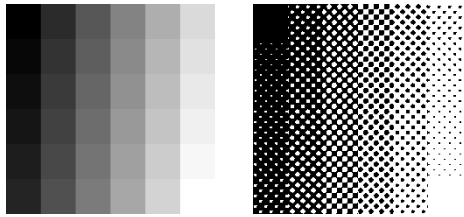


## Lecture 11

### Halftoning

Cluster Dot Dithering  
Disperse Dot Dithering  
Error Diffusion  
Color Halftoning  
Color Screening



## Monochrome Printing

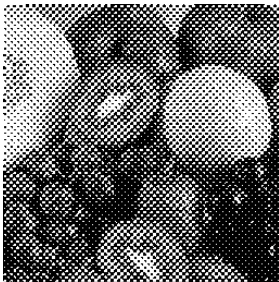
GrayScale



Threshold



## Halftoning (Screening)



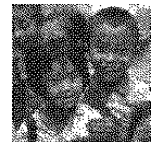
## Halftoning



GrayScale



Threshold



Halftone

Local average  
gray in halftone image  $\approx$  Local average  
gray in grayscale  
image

### Physical Screening

Larger hole in screen -> more ink goes through

See demo:  
[http://www.ted.photographer.org.uk/photoscience\\_halftones.htm](http://www.ted.photographer.org.uk/photoscience_halftones.htm)

### Physical Screening

Gradient exposure

Larger hole in screen -> more light goes through

### Halftoning

Percentage of ink coverage of a region determines the grayscale:

	gray = 0.7	gray = 0.5	gray = 0.3	
....				....
....				....
....				....

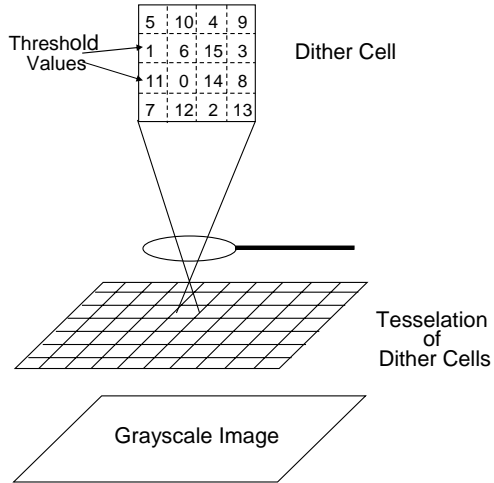
### Halftoning Methods

- 1) Dithering
- 2) Error diffusion
- 3) Direct Binary Search  
(Iterative - error minimization)

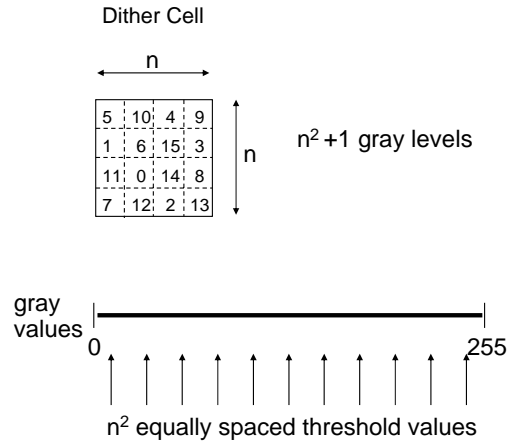
Proportion of local ink coverage in halftone image  $\approx$  Local average gray in grayscale image

## Dithering

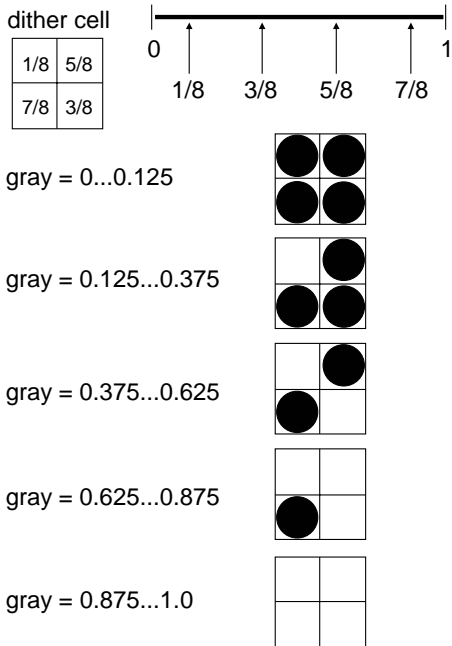
Every pixel in a region is thresholded using a different threshold value.



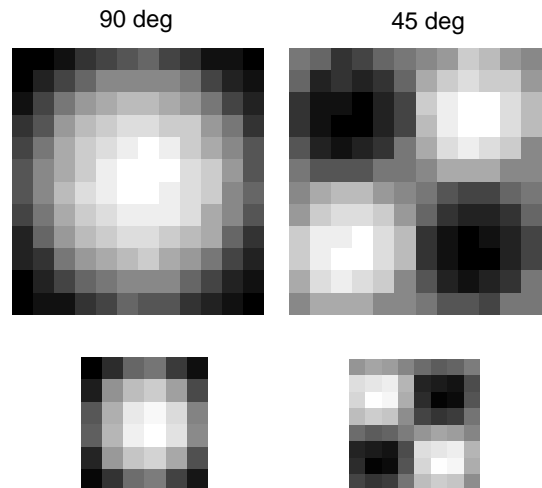
## Threshold Values in Dither Cell



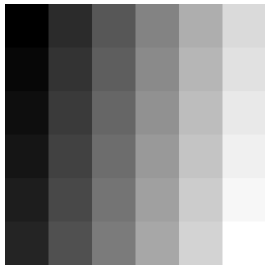
Example:



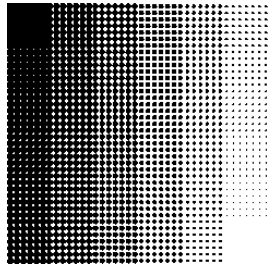
## Cluster Dot Dither Cells



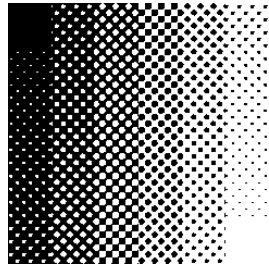
### Cluster Dot Dither Cells



Grayscale



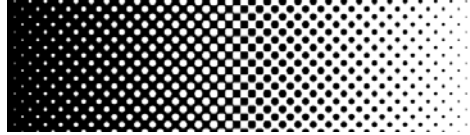
C<sub>6</sub> 90 deg



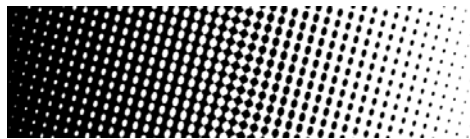
C<sub>12</sub> 45 deg

### Cluster Dot Dithering

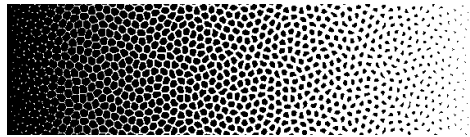
Clustered Dot Postscript Screens



Rotated Elliptical



Hybrid FM Clustered Dot

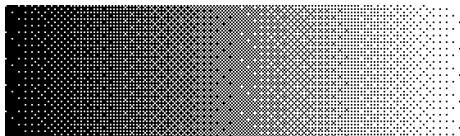


### Dispersed Dot Dithering

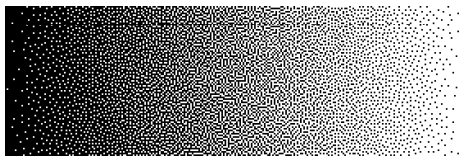
True Random



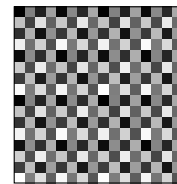
Bayer = perfectly smooth



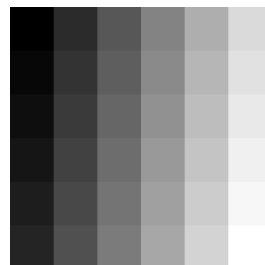
Blue Noise



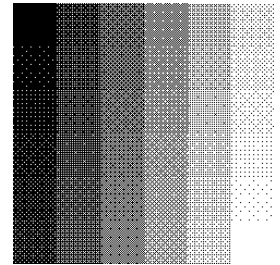
### Bayer Dithering



Bayer Dither Cell



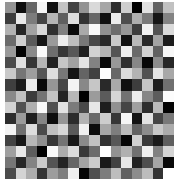
Grayscale



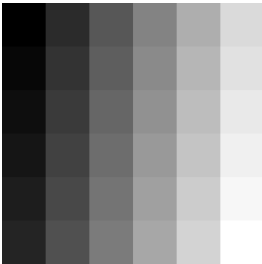
Bayer Dither

(Bayer, 1973)

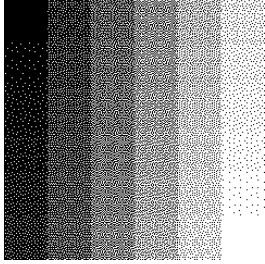
### Void and Cluster Dithering



Void & Cluster  
Dither Cell



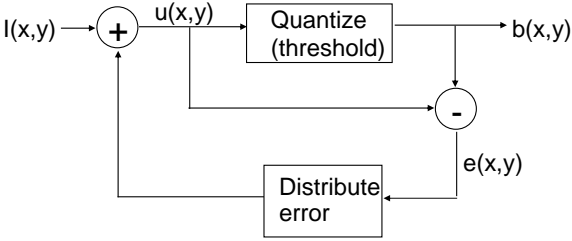
Grayscale



Void & Cluster Dither

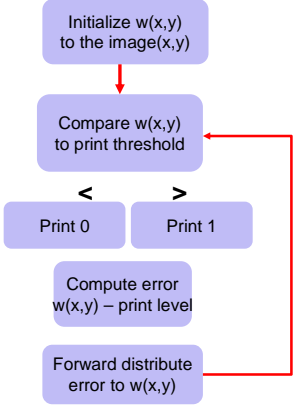
(Ulichney 1993)

### Error Diffusion (Floyd Steinberg)



(Floyd and Steinberg 1976)

### Error Diffusion (Floyd Steinberg)



- Decide for each image point whether to print or not
- Take error between the desired output at that position and the printed level.
- Distribute that error forward to pixels yet-to-be printed

### Example: 1D error diffusion

$I = [0.7 \quad 0.7 \quad 0.3 \quad 0.5 \quad 0.1 \quad 0.1 \quad 0.1]$

$I(1) = u(1) = 0.7 \rightarrow \text{threshold at } 0.5 \rightarrow b(1) = 1$

$e(1) = b(1) - u(1) = 0.3$

Since pixel  $I(1)$  was over represented, compensate by subtracting error from next pixel  $I(2)$

$u(2) = I(2) - e(1) = 0.4$

$u(2) = 0.4 \rightarrow \text{threshold at } 0.5 \rightarrow b(2) = 0$

$e(2) = b(2) - u(2) = -0.4$

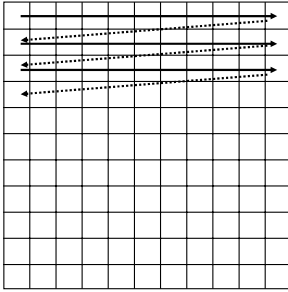
$u(3) = I(3) - e(2) = 0.7$

and so on....

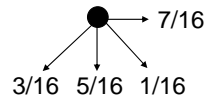
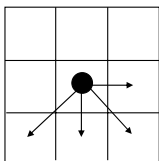
$b = [1 \quad 0 \quad 1 \quad 0 \quad 0 \quad 0 \quad 1]$

## Error Diffusion in 2D

Scan Image:



error diffusion

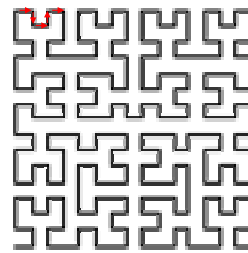


## Error Diffusion - Variations

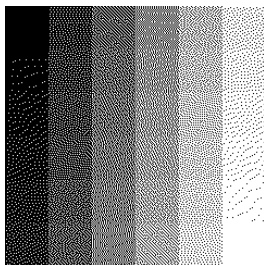
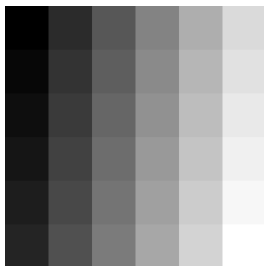
Jarvis Judice and Ninke (1976)  
Error diffused differently

		*	7	5
3	5	7	5	3
1	3	5	3	1

Terada, Tamura, and Saito  
Use Peano scan (Space filling curve)



## Error Diffusion



## Error Diffusion



## Direct Binary Search (DBS)

Given an error metric:

$$d(l(x,y),b(x,y))$$

example:  $d(l,b) = \sum((l(x,y)-b(x,y))^2)$

Initialize binary image  $b(x,y)$  (example - choose random binary image).

Randomly chose a pixel  $(x_0,y_0)$  in  $b(x,y)$

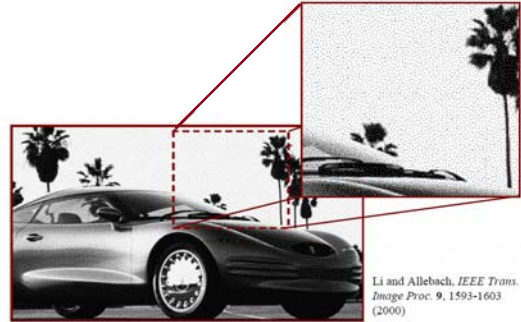
if  $d(l,\bar{b}) < d(l,b)$  then assign  $b = \bar{b}$

where  $\bar{b}$  is  $b$  except for  $\bar{b}(x_0,y_0) = 1-b(x_0,y_0)$

Repeat last step until  $|d(l,b) - d(l,\bar{b})|$  is "small".

Error metric can be "smart" for example based on Human Visual System.

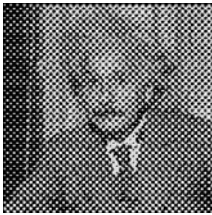
## Direct Binary Search (DBS)



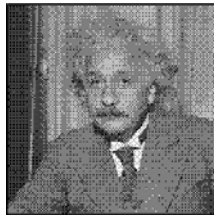
Li and Allebach, *IEEE Trans. Image Proc.* 9, 1593-1603 (2000)

## Halftoning - Comparison

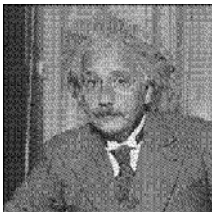
Cluster Dot



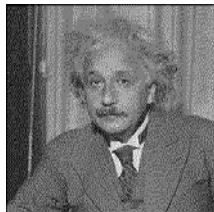
Bayer



Void and Cluster

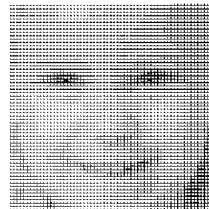


Error diffusion

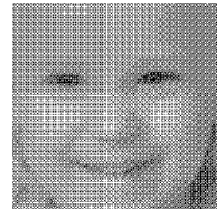


Comparison of various halftoning:  
<http://www.cs.indiana.edu/~dmiguse/Halftone/>

## Halftoning - Comparison



Clustered Dot Screening  
AM Halftoning



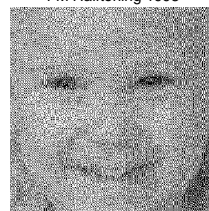
Dispersed Dot Screening  
FM Halftoning



Blue-noise Mask  
FM Halftoning 1993



Green-noise Halftoning  
AM-FM Halftoning 1992

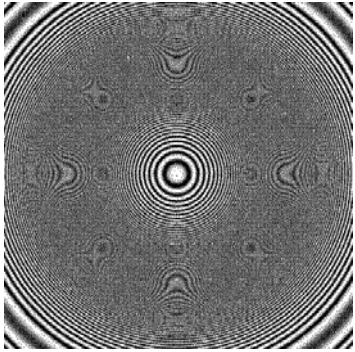


Error Diffusion  
FM Halftoning 1975



Direct Binary Search  
FM Halftoning 1992

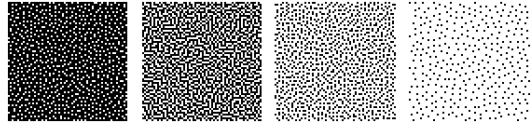
### Aliasing - Moire



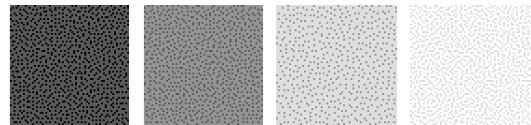
Aliasing due to dot overlap (DBS method)

### Variable Dot Size

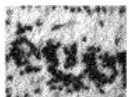
#### Fixed Dot Halftoning (On or Off)



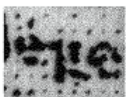
#### Variable Dot Halftoning (4 different dot sizes)



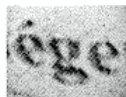
### Variable Dot Size



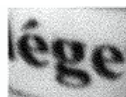
Ink Jet



Thermal transfer



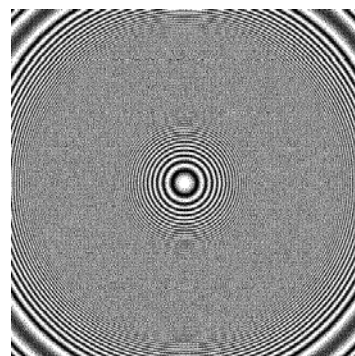
Variable dot Thermal transfer



Dye diffusion

(Moroney and Viggiani 1994)

### Aliasing Removed



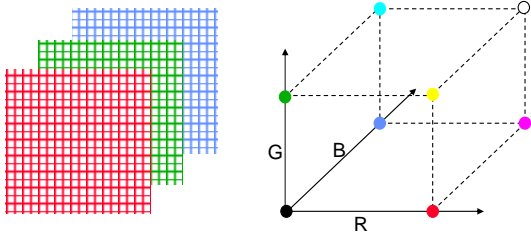
Aliasing Removed using variable dot size (dot overlap model).

(Baquai, Taylor and Allebach 1996)



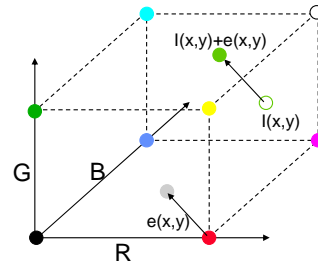
### Color Halftoning

- 1) Perform halftoning in each plane (R,G,B) separately.
- 2) Perform halftoning in color space



### Error Diffusion in RGB Space

The error  $e(x,y)$  - is a vector



Adding and subtracting is in 3D vector space.

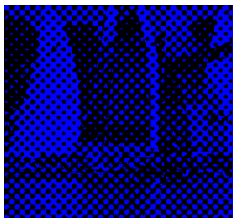
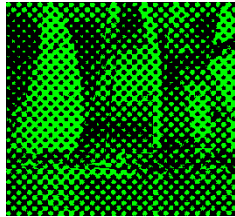
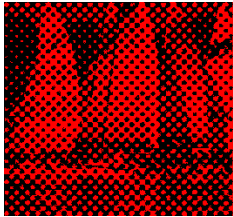
### Error Diffusion in Color Images



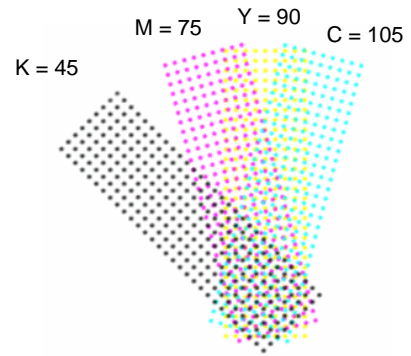
### Error Diffusion in Color Images



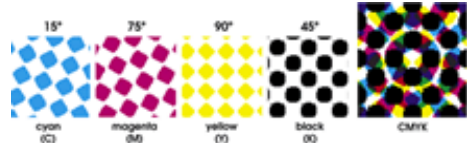
## Cluster Dot Dithering in Color Images



## Color Screen Angles

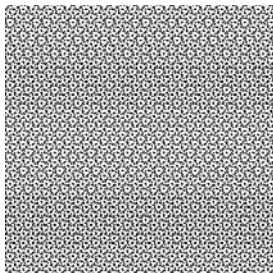


- Every screen at a different angle.
- Optimally 30° apart.
- Since there are 4 screens and not 3:  
Y (colour of least contrast) is set at 15° between 2 others.
- K (colour of most contrast) is set at the visually ideal angle of 45 degrees.

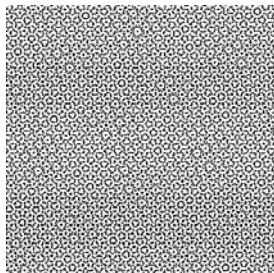


## Color Screening

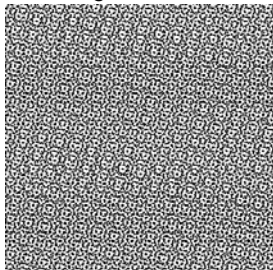
CMK Rosetes



Failed CMK Rosettes



15 deg Yellow Moire



Final Print

