

# Segmentation

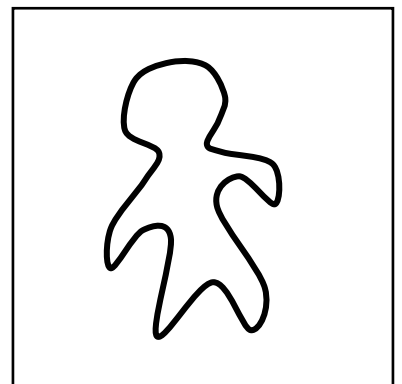
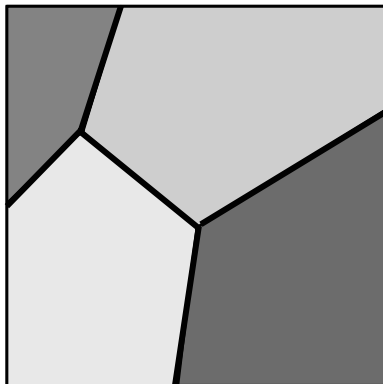
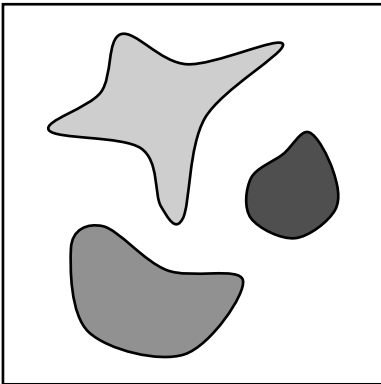
- Threshold Segmentation
  - Local thresholding
  - Edge thresholding
  - Threshold using averaging
  - Gradient Detectors
- Region Growing
- Split & Merge
  
- Shape Matching
- Shape Representation



# Segmentation

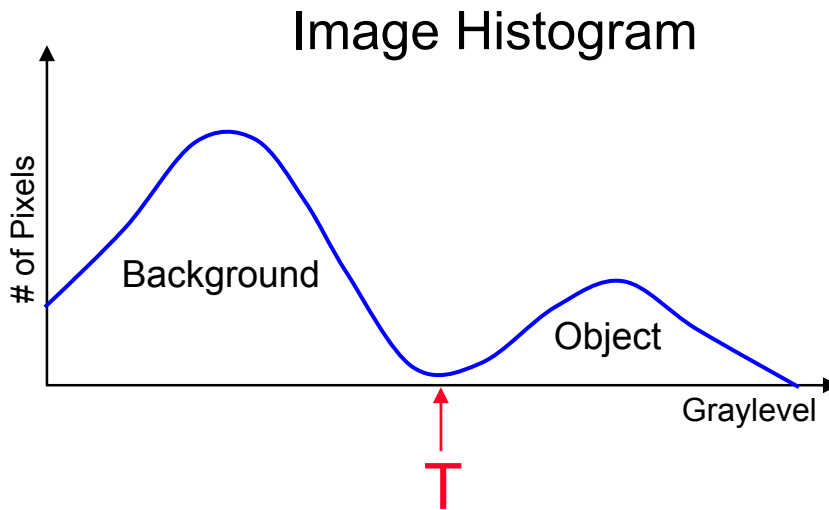
**Image Segmentation** = divide image into (continuous) regions or sets of pixels.

- 1) Region Based
- 2) Boundary Based
- 3) Edge Based



# Thresholding

**Global Thresholding** = Choose threshold  $T$  that separates object from background.

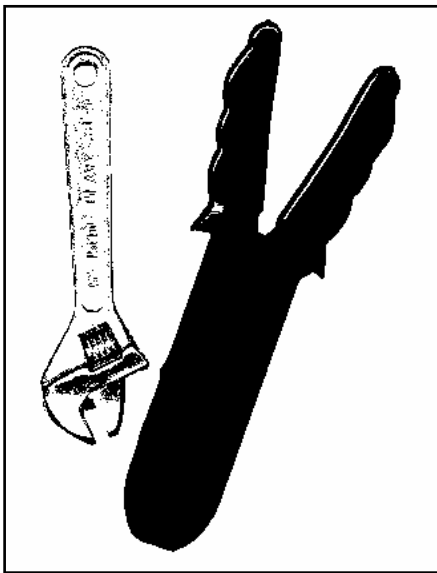
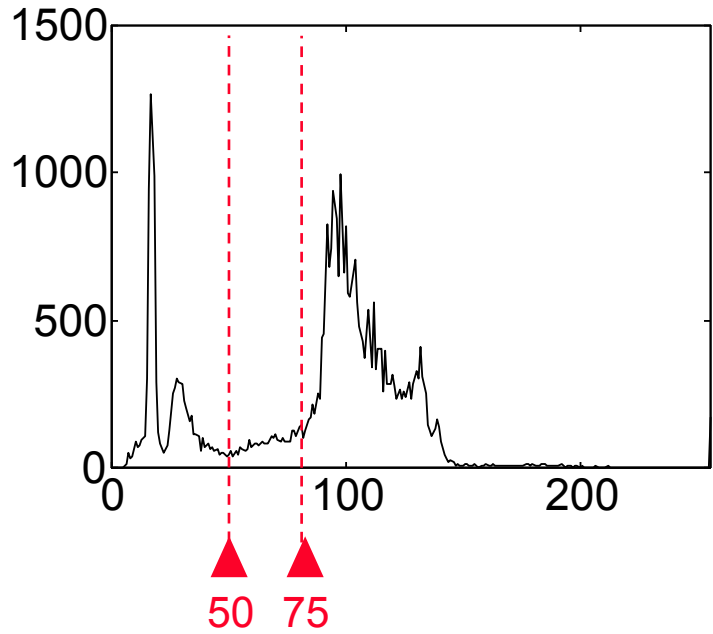


# Segmentation using Thresholding

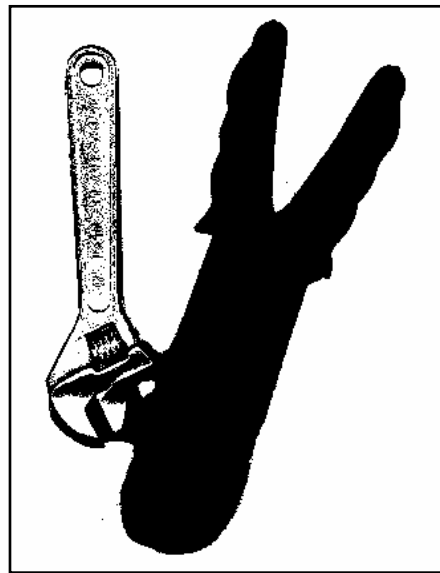
Original



Histogram



Threshold = 50

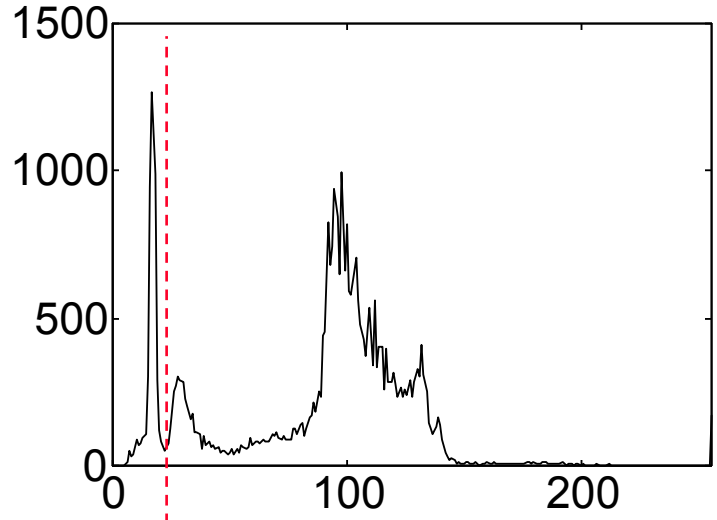


Threshold = 75

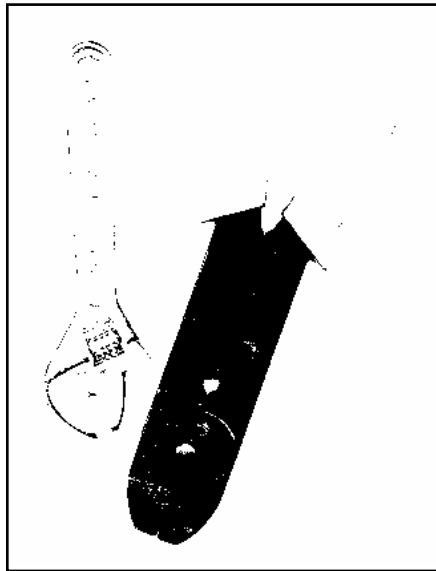
Original



Histogram



21



Threshold = 21

# Thresholding a Grayscale Image

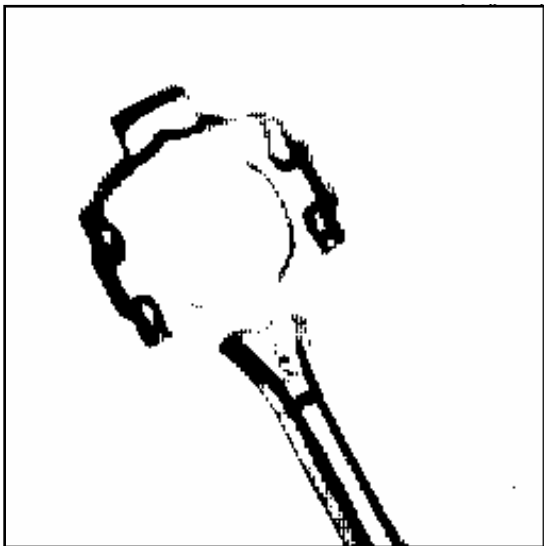
Original Image



Thresholded Image



Threshold too low

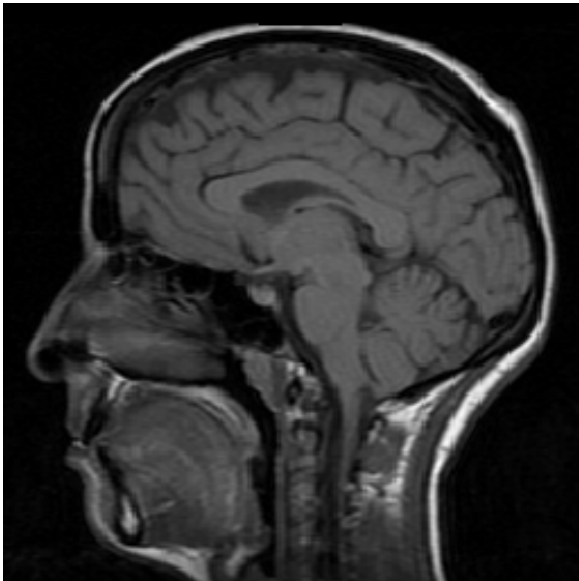


Threshold too high



# FMRI - Example

Original Image



Threshold = 80

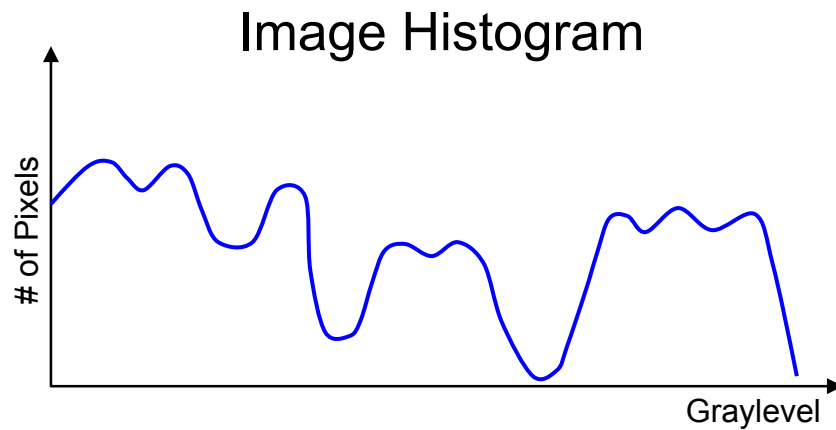


Threshold = 71



Threshold = 88

Simple thresholding is not always possible:

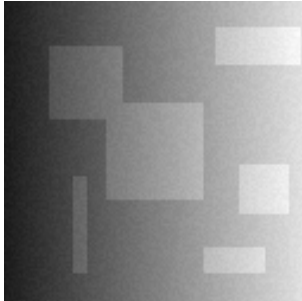


- 1) Many objects at different gray levels.
- 2) Variations in background gray level.
- 3) Noise in image.

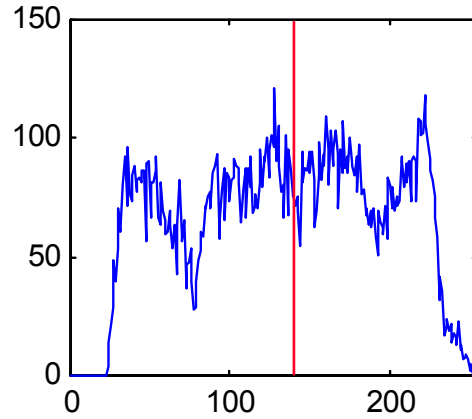


# Thresholding Example

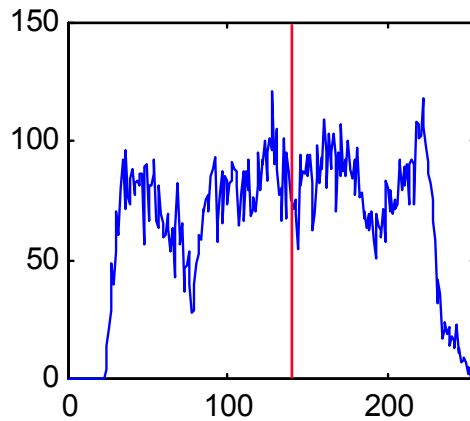
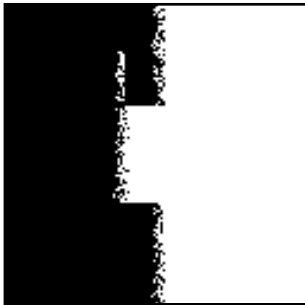
Original



Histogram



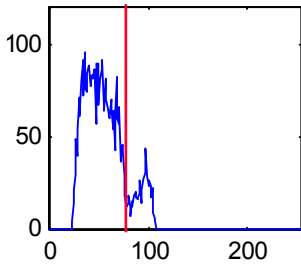
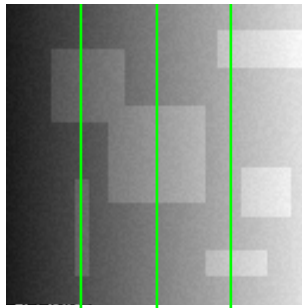
## Single Global Threshold



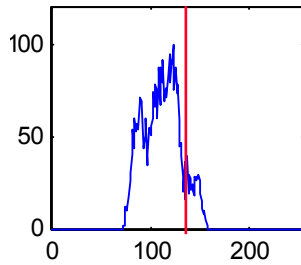
$T = 128$

# Local Thresholding - 4 Thresholds

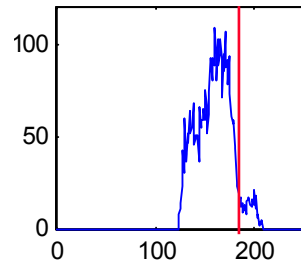
Divide image in to regions. Perform thresholding independently in each region.



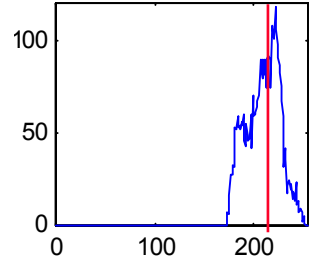
$T = 80$



$T = 128$



$T = 188$

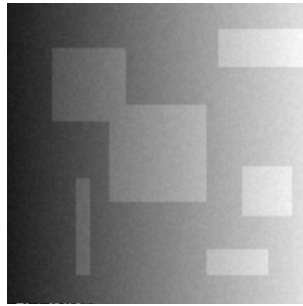


$T = 226$

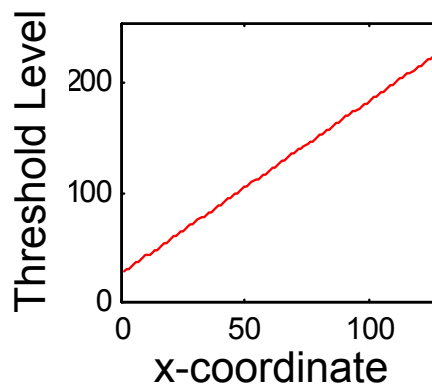


# Adaptive Thresholding

Every pixel in image is thresholded according to the histogram of the pixel neighborhood.

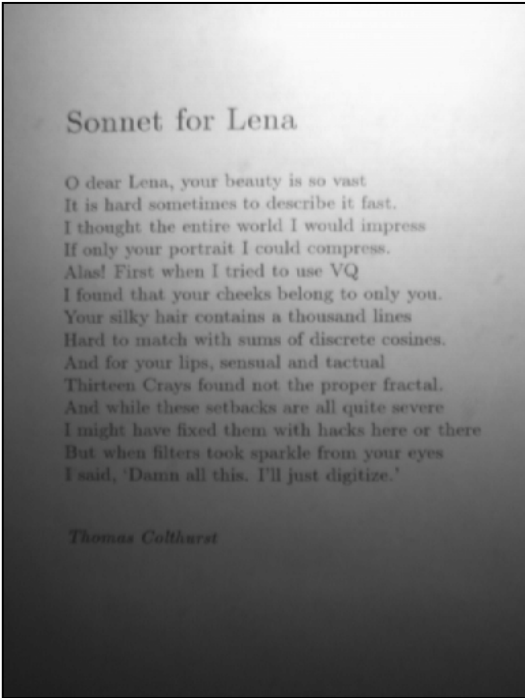


**T =**

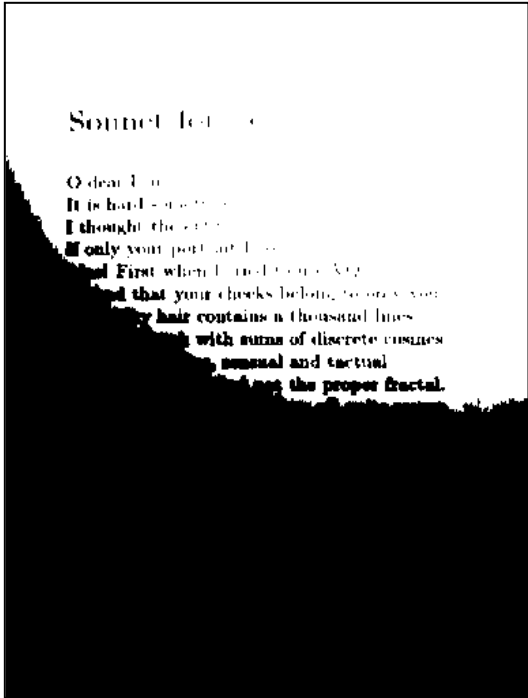


# Adaptive Thresholding - Example

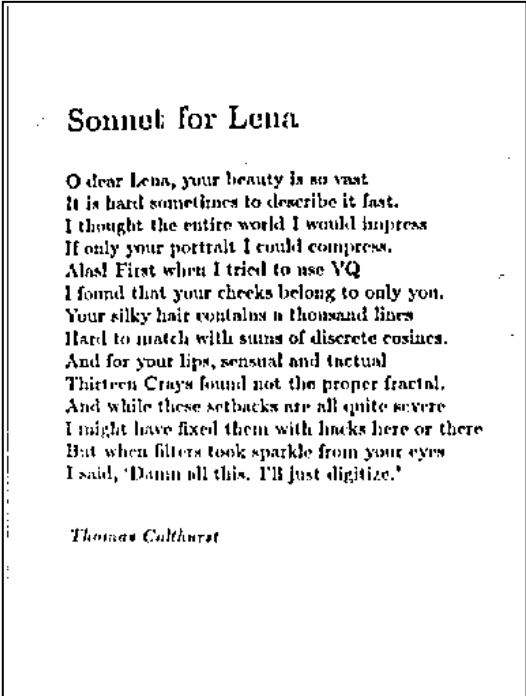
## Original



## Global Threshold

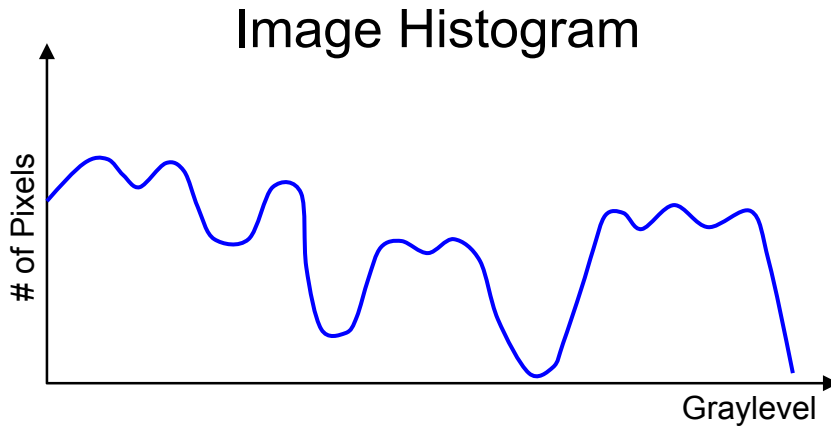


## Adaptive Threshold

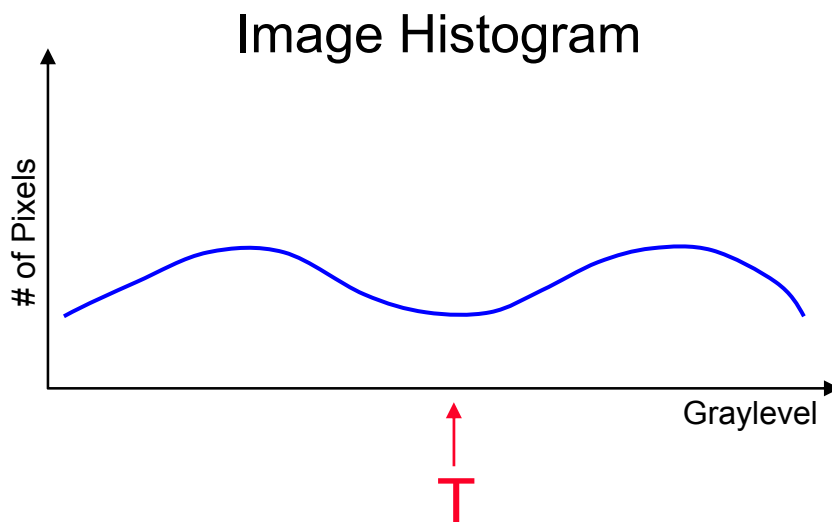


# Threshold Segmentation of Noisy Images

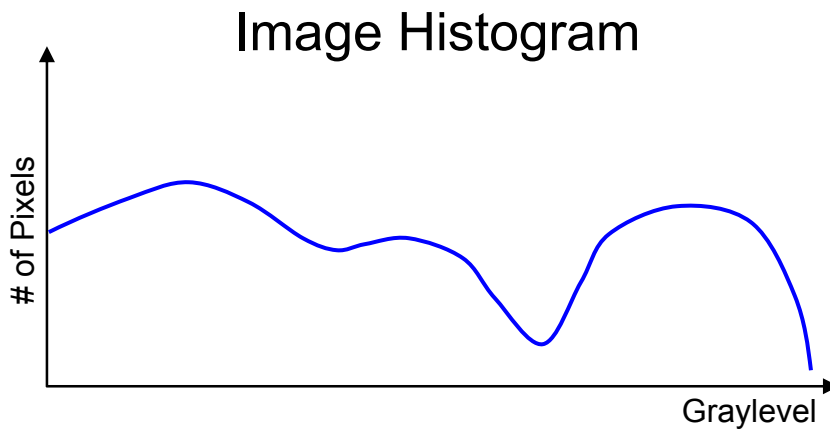
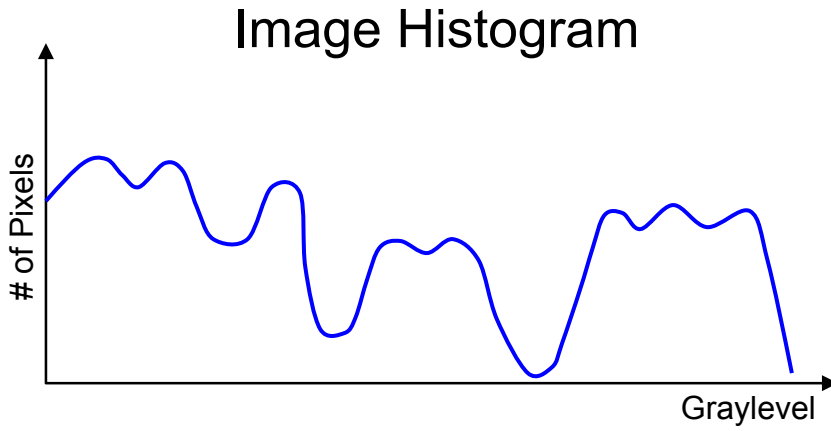
Noise inhibits localization of threshold.



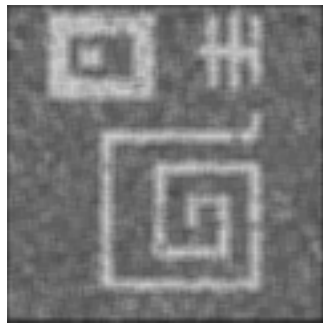
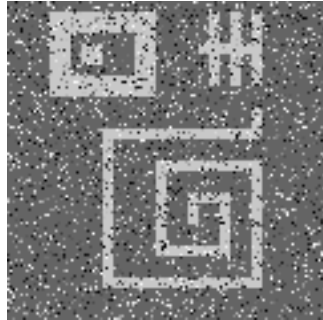
Smooth image and obtain a histogram for which threshold is easily determined.



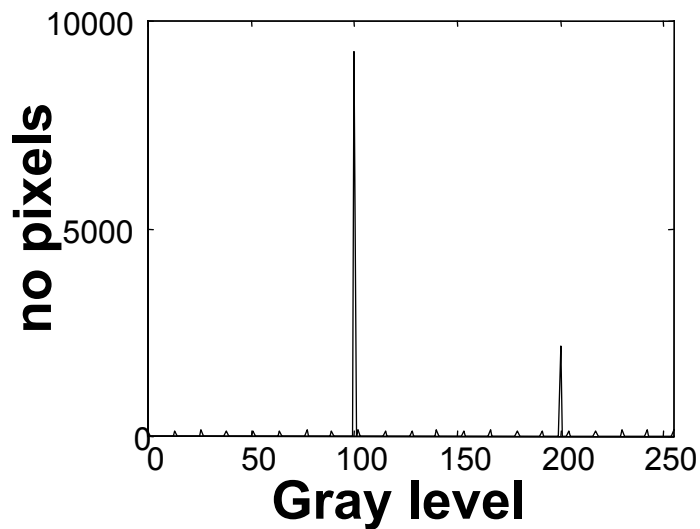
Note: Smooth the image, not the histogram...



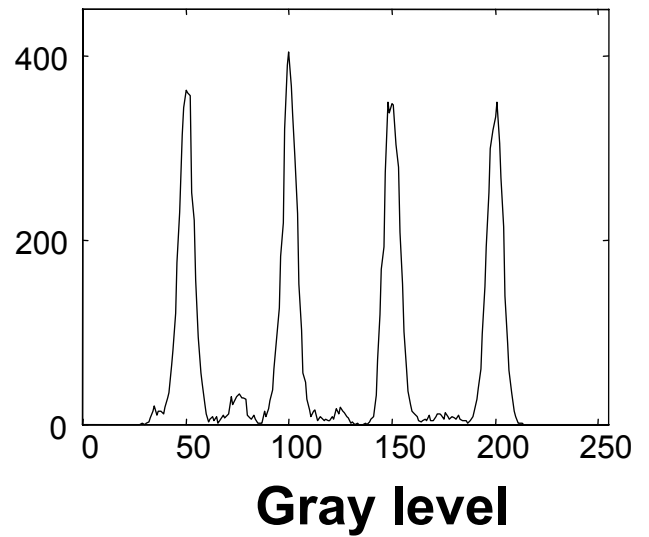
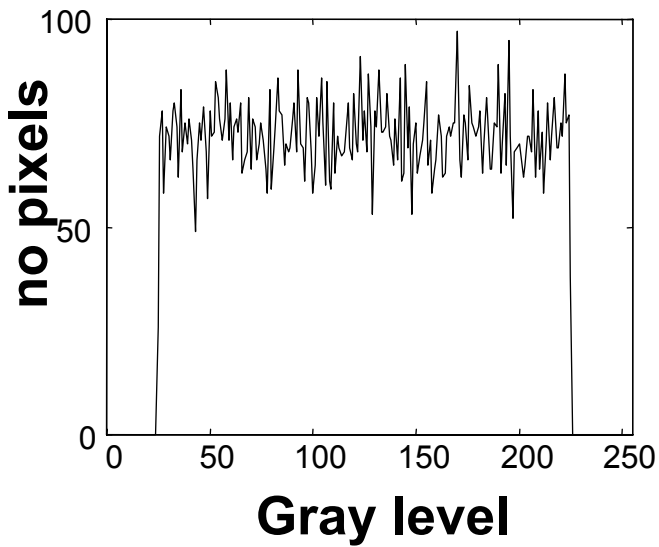
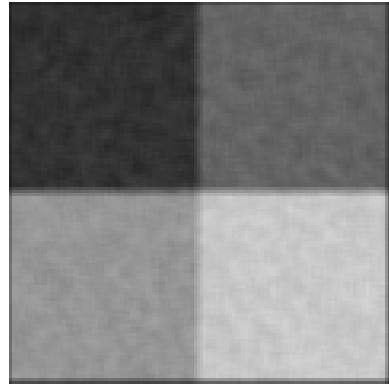
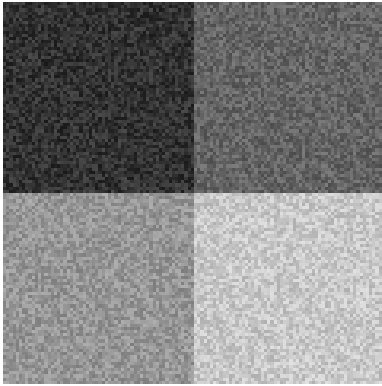
# Threshold using Average



## Gray level Histograms



# Threshold using Average

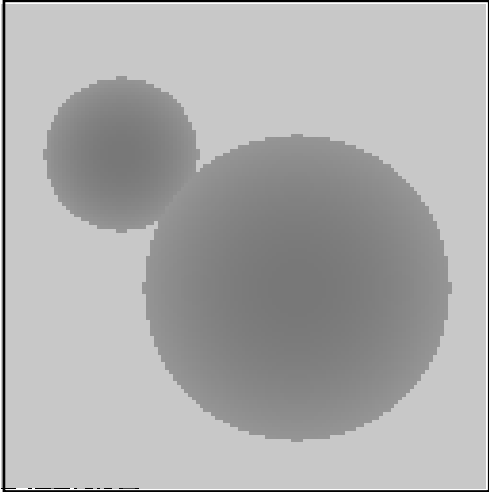


**Gray level Histograms**

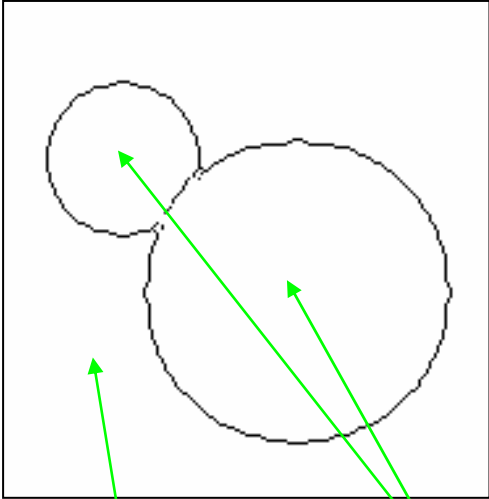


# Edge Based Segmentation

Original



Edge Image

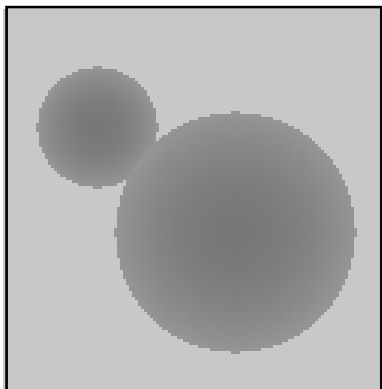


Background

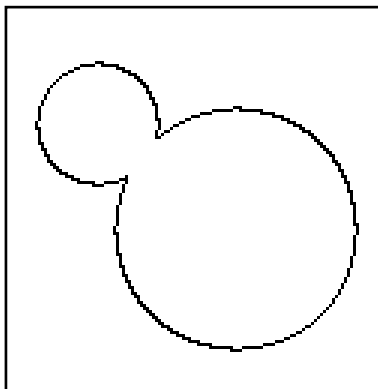
Object

# Edge Based Thresholding

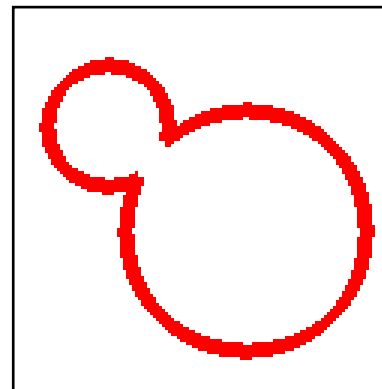
Original



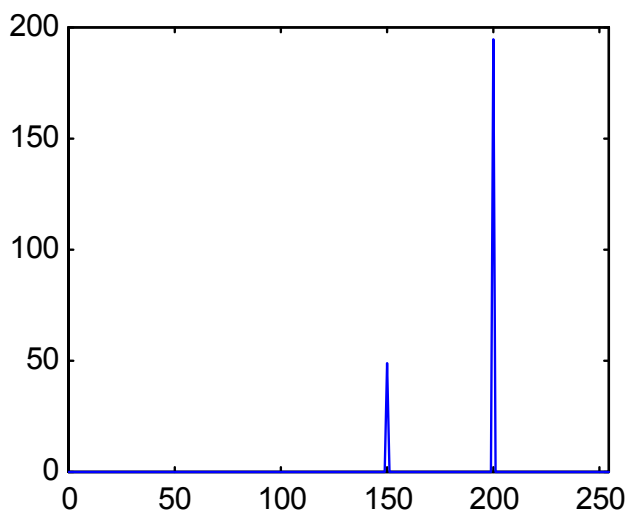
Edge Pixels



Edge Neighbors

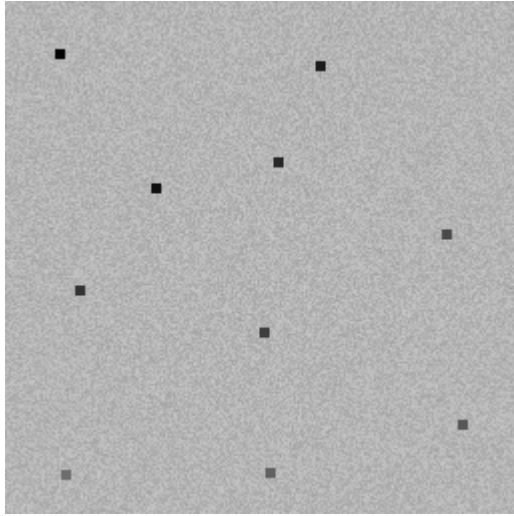


Edge Neighbors Histogram

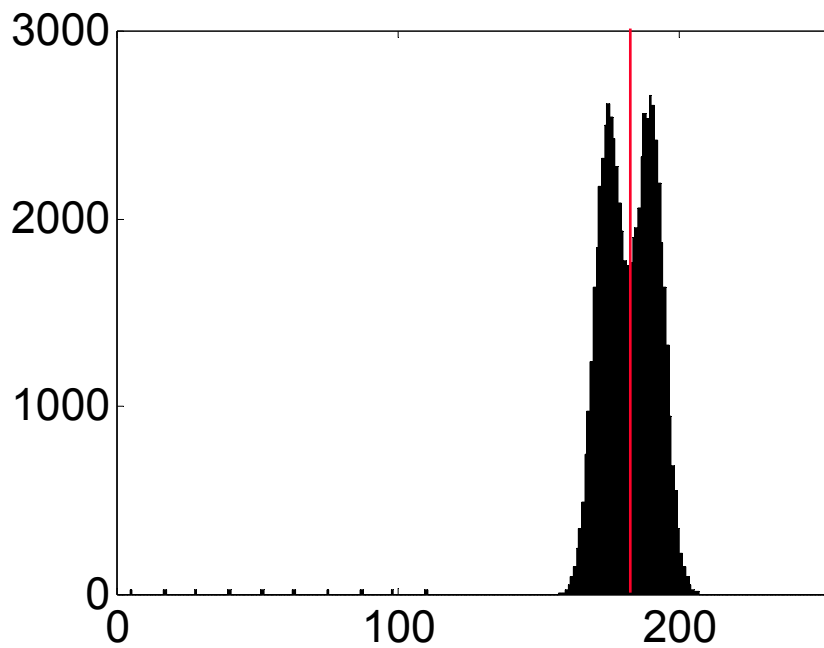
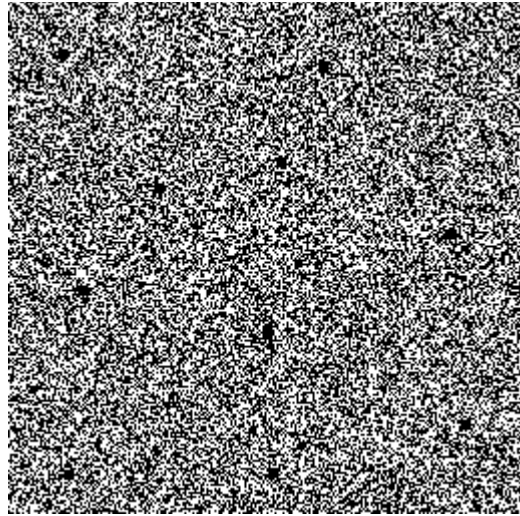


# Thresholding Based on Boundary Characteristics

Original



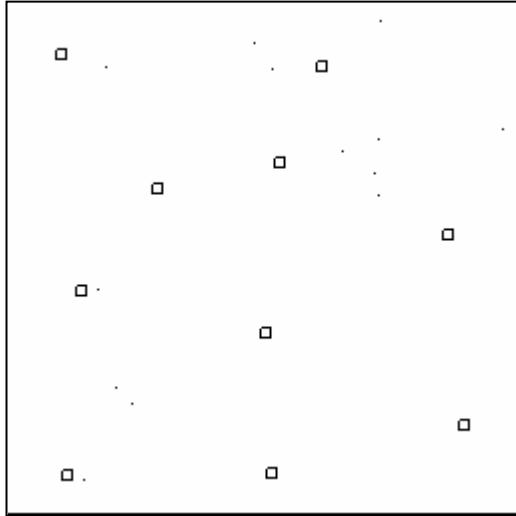
Threshold (T=182)



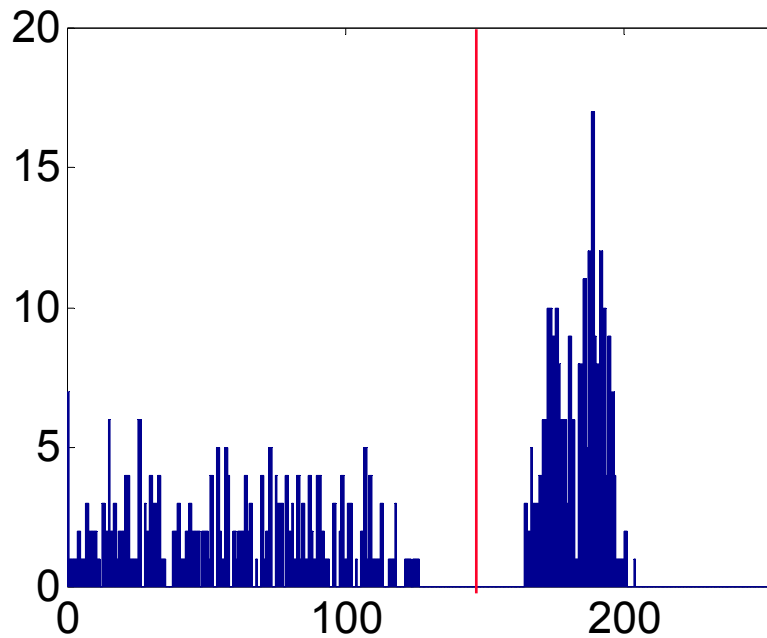
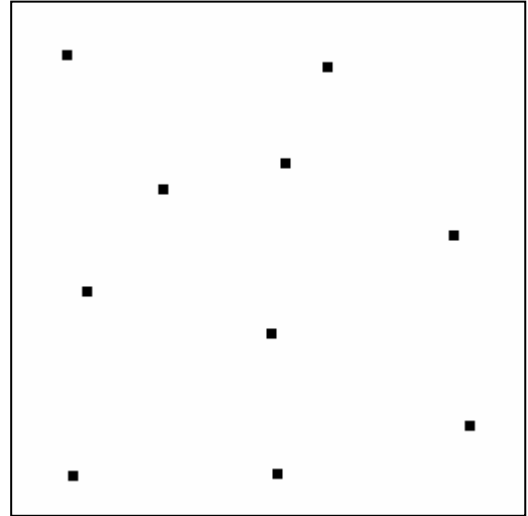
Global Histogram

# Thresholding Based on Boundary Characteristics

Original



Threshold (T=143)



Edge Neighborhood Histogram

# Region Growing

## Define:

$S$  = the set of pixels inside the region.

$Q$  = queue of pixels to be checked.

$(x_0, y_0)$  = a pixel inside the region.

## Algorithm:

Initialize:  $S = \emptyset$

$Q = \{ (x_0, y_0) \}$

1) Extract pixel  $P$  from queue  $Q$

2) Add  $P$  to  $S$ .

3) For each neighbor  $P'$  of  $P$ :

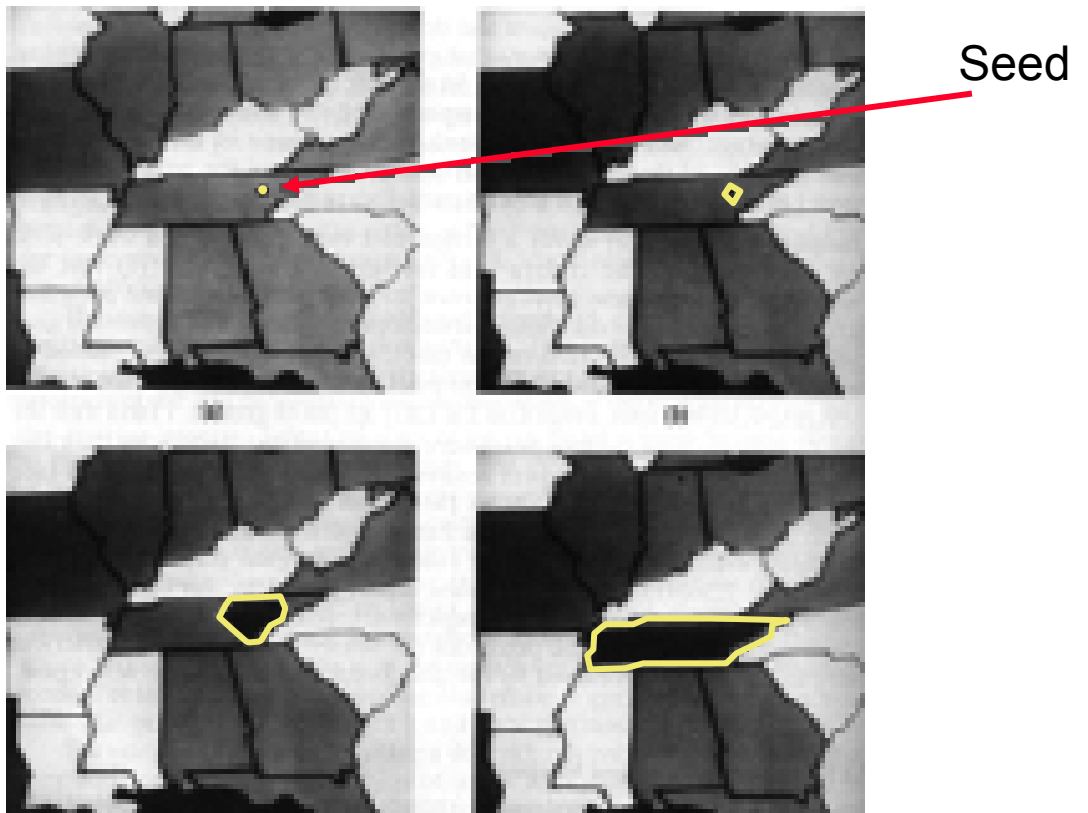
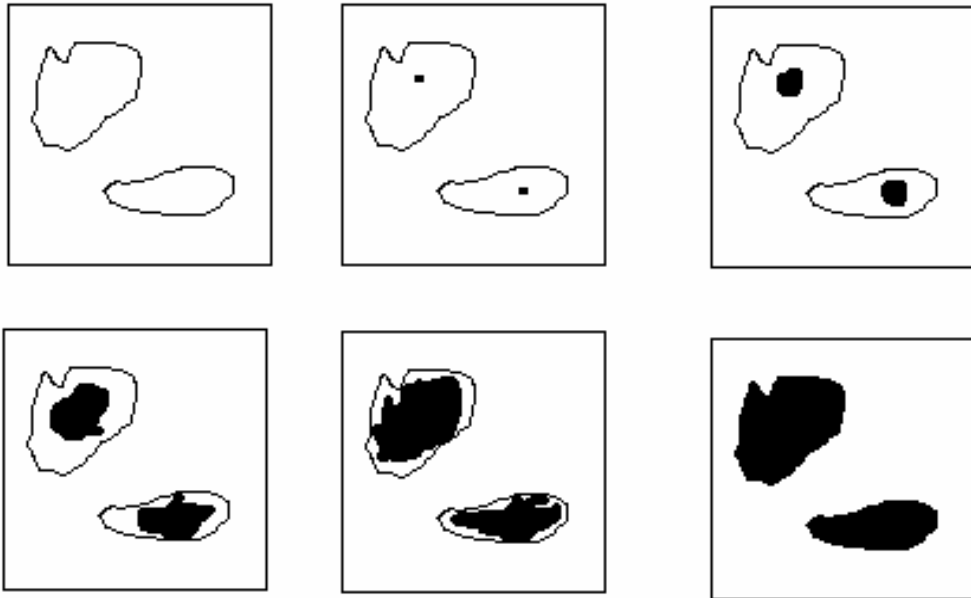
if  $P'$  is "similar" to  $P$  and  $P' \notin S$  then

add  $P'$  to  $Q$ .

4) If  $Q = \emptyset$  then end, else return to 1.

$S$  = the extracted pixels of the region.  
Define what "similar" means.  
Problematic in small gradient regions.

# Region Growing - Example

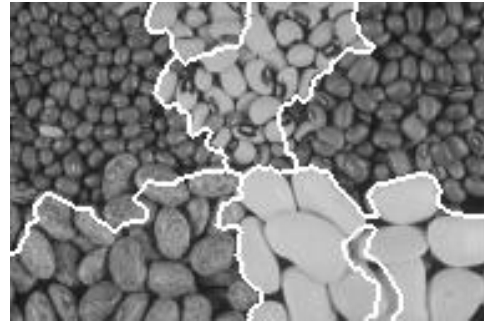


# Region Growing - Examples

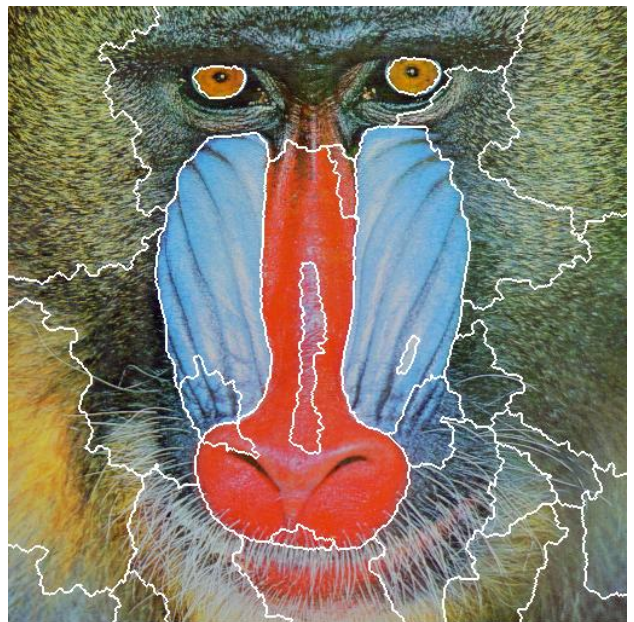
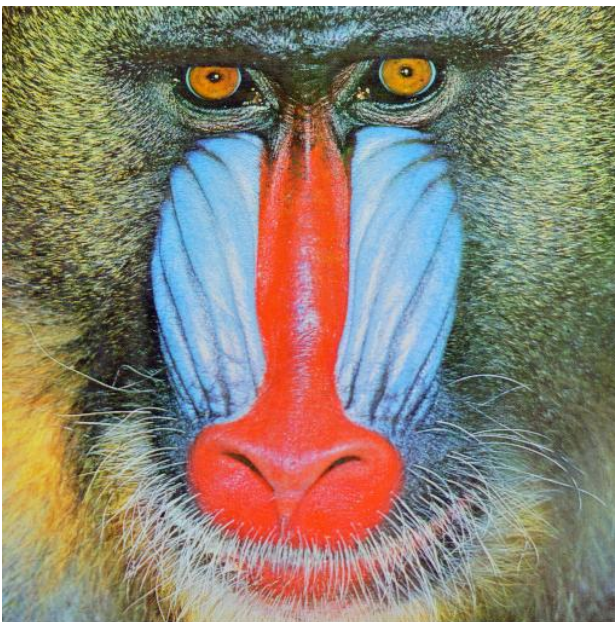
## Color Segmentation



## Texture Segmentation

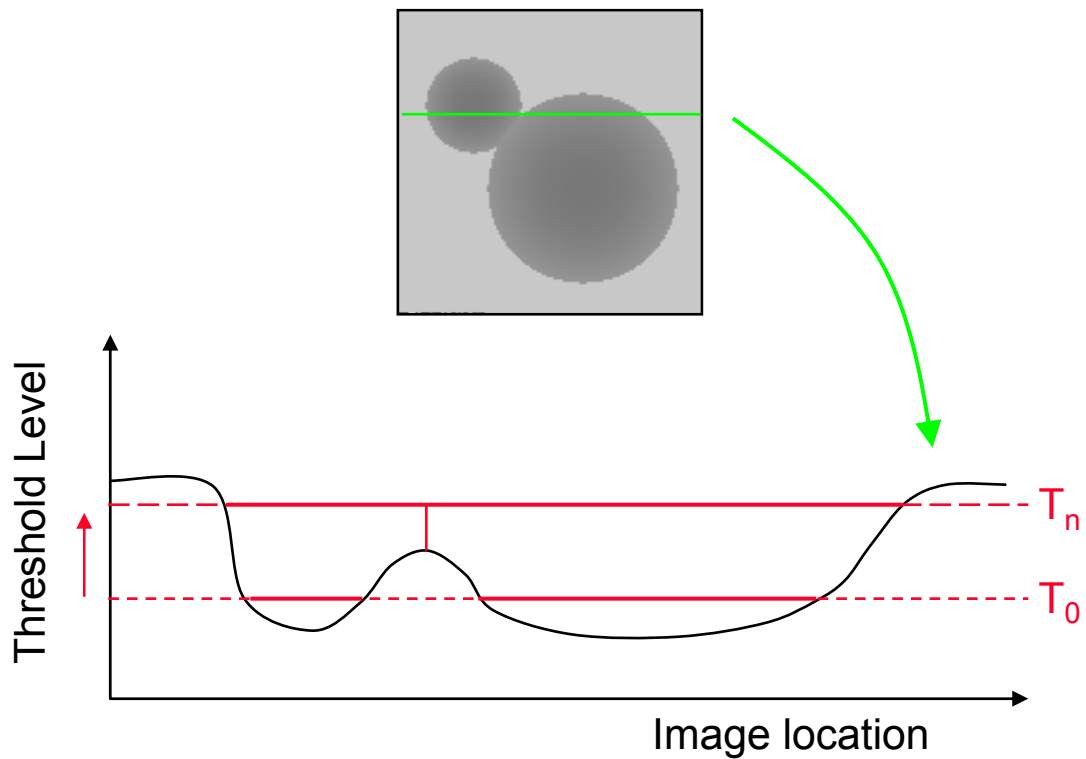
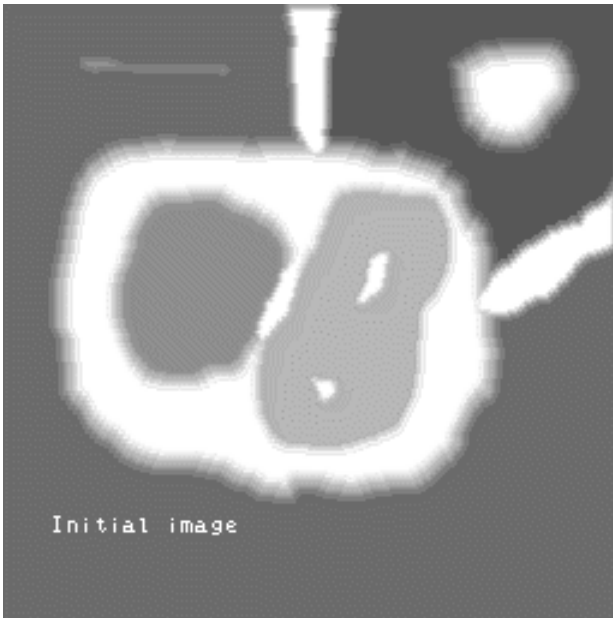


## Color + Texture Segmentation



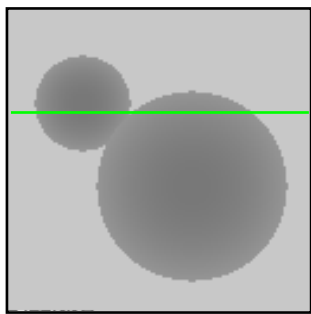
# Watershed Threshold Algorithm

An Image can be viewed as a topographic map

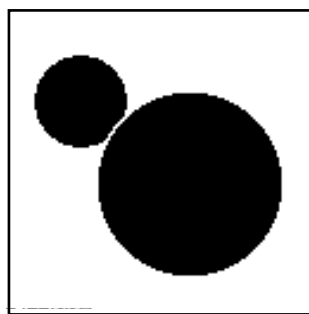




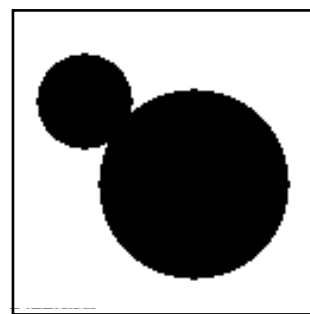
# Watershed Threshold Algorithm



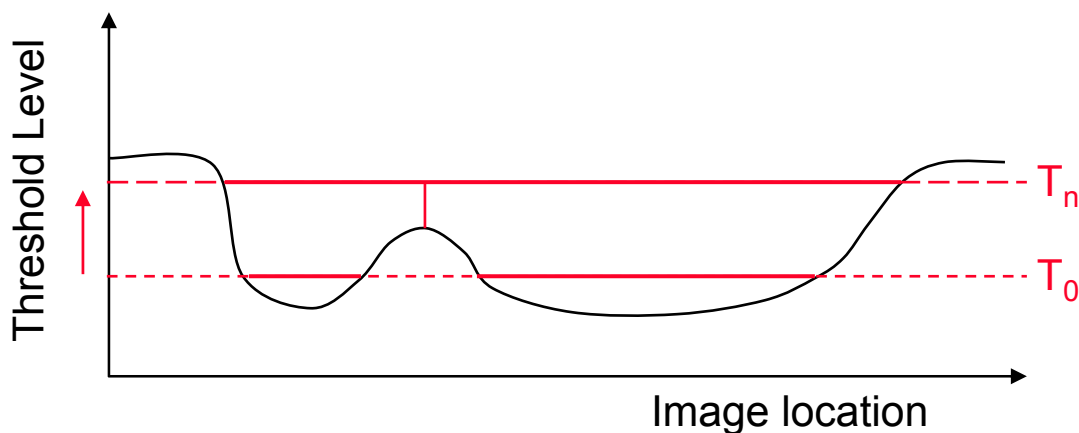
Original



$T = 149$

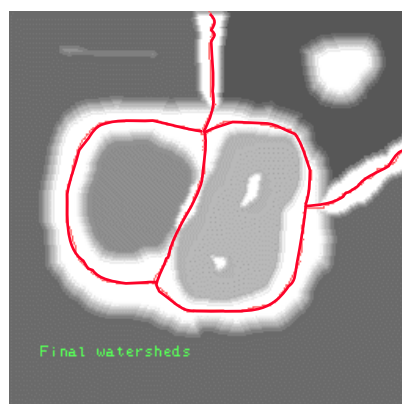
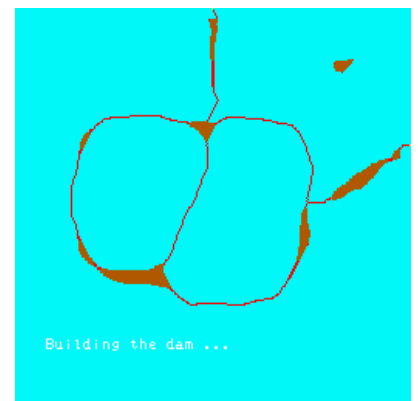
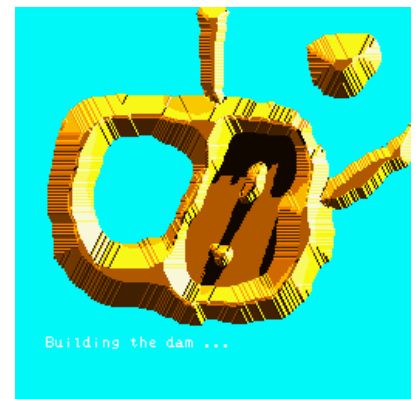
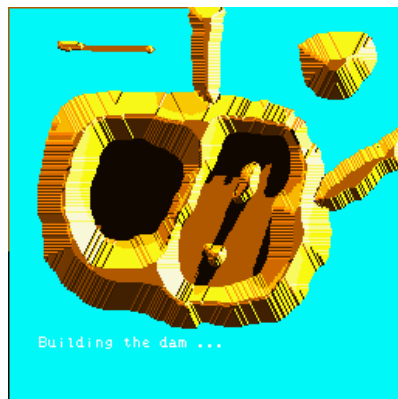


$T = 150$



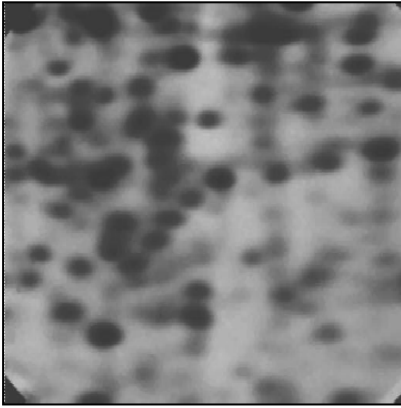
Initialize threshold at  $T_0$  that separates objects well.  
Determine connected components.  
Raise threshold, and detect pixels that pass threshold and belong to more than one connected component.  
Do not let objects merge.  
Set these pixels as object boundaries.

# Watershed Threshold Algorithm

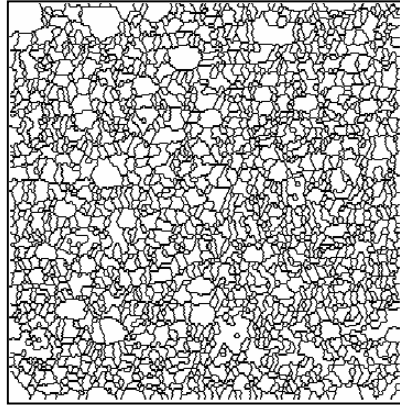


# Watershed Threshold Algorithm

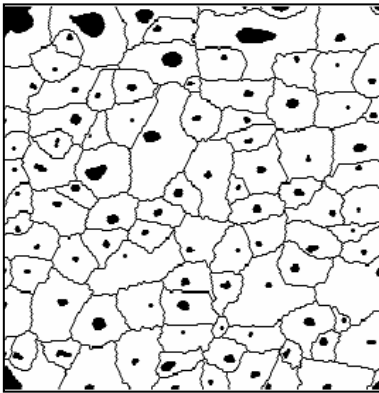
Original



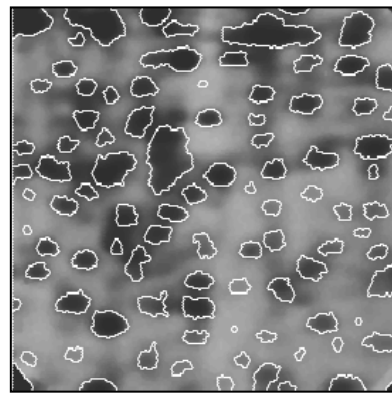
Watershed Boundaries



Watershed Markers



Watershed Boundaries



Watershed Markers may be chosen manually or local global maximas (as above)

# Split & Merge Segmentation

## 2 Stage Algorithm:

### Stage 1: Split

Split image into regions using a Quad Tree representation.

### Stage 2: Merge

Merge "leaves" of the Quad Tree which are neighboring and "similar".

Original



Split



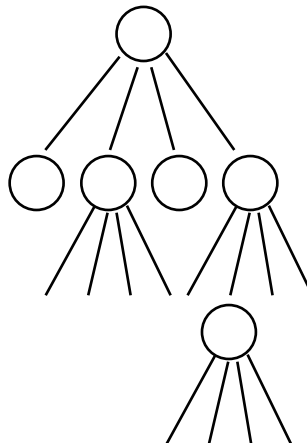
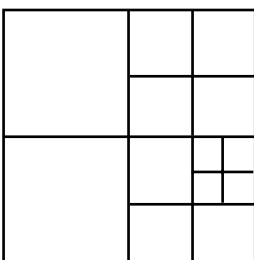
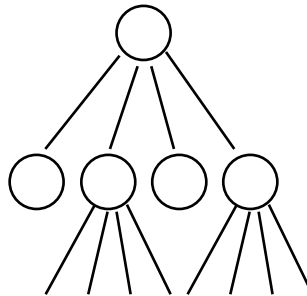
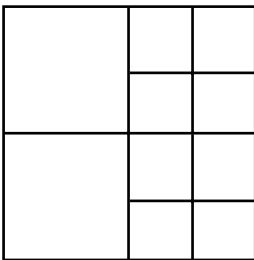
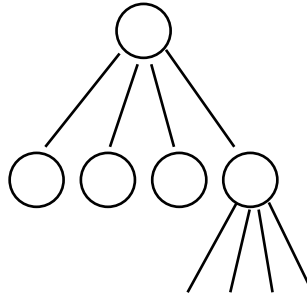
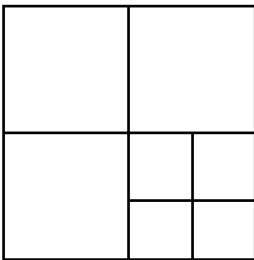
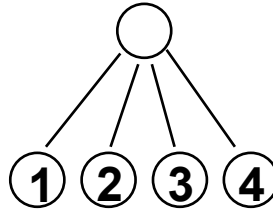
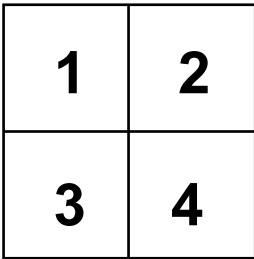
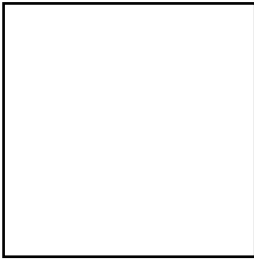
Split + Merge



# Quad Tree - Representation

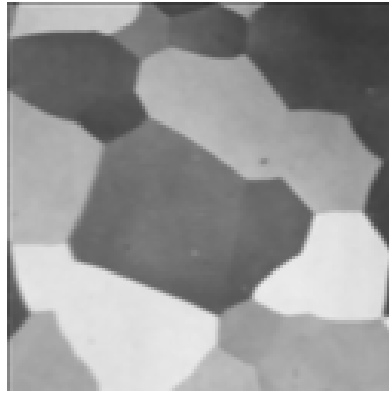
Image

Quad Tree

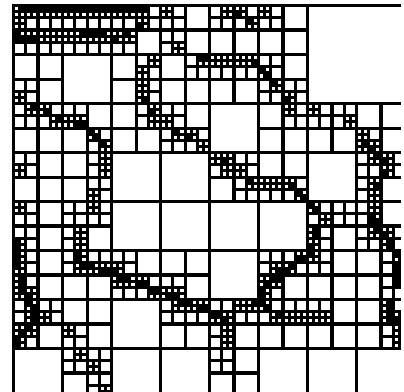
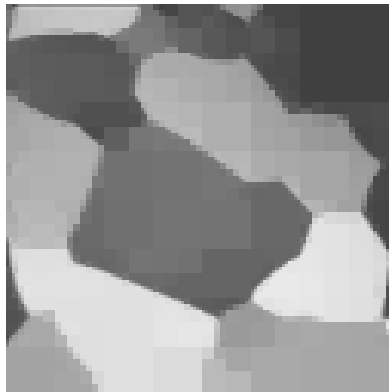


# Quad Tree Representation

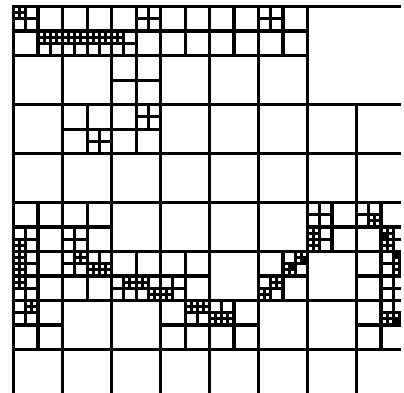
Original



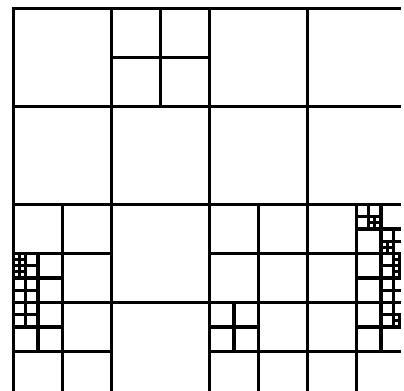
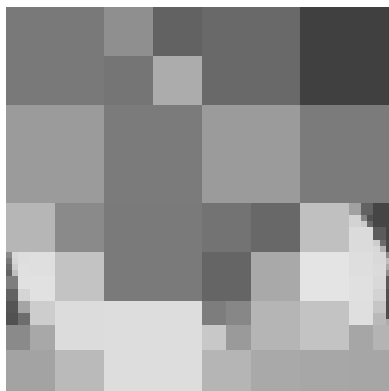
Thresh = 0.20



Thresh = 0.40

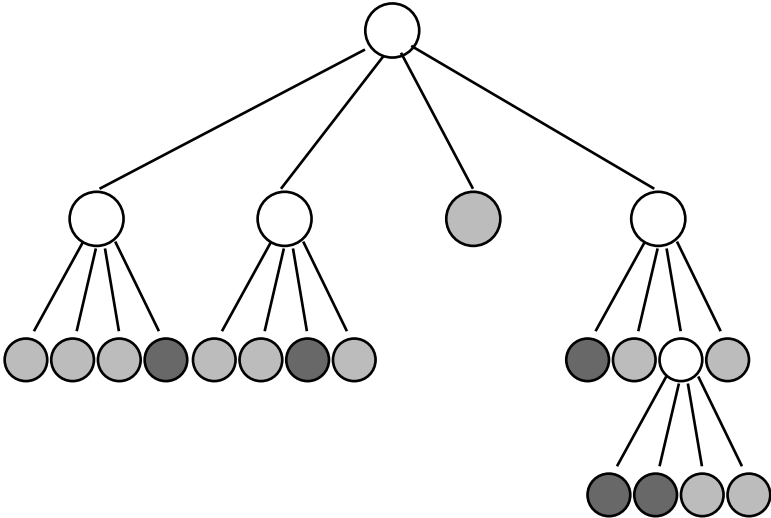
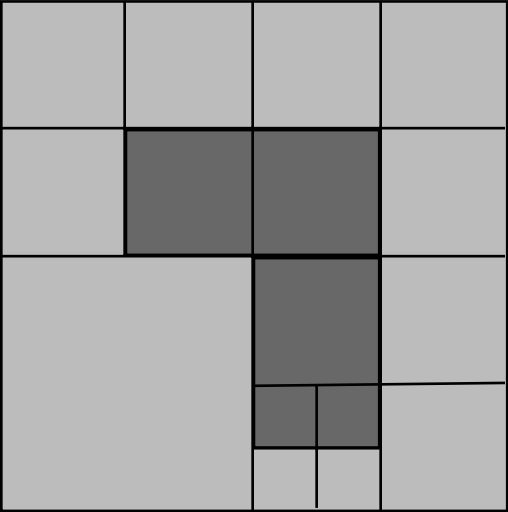


Thresh = 0.55

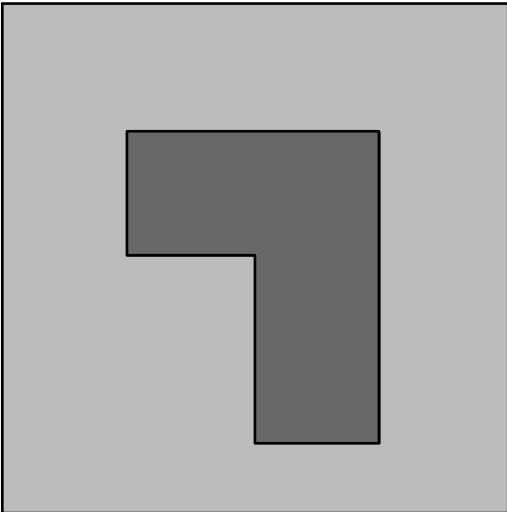


# Split & Merge Example

## Stage 1: Split



## Stage 2: Merge

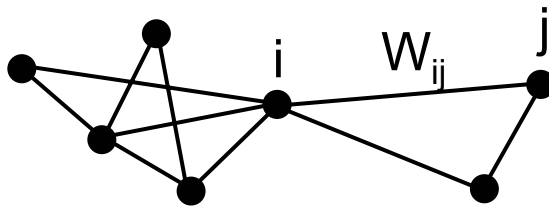
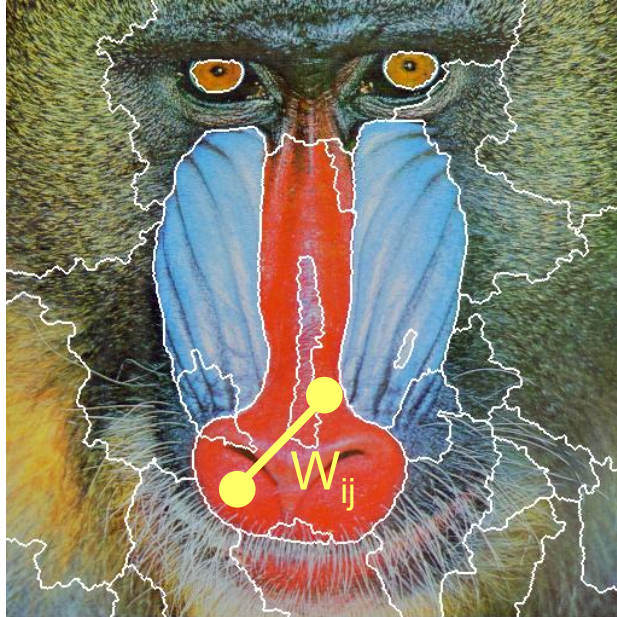


# Split & Merge Example





# Graph-Cut Segmentation



$$G = \{ V, E \}$$

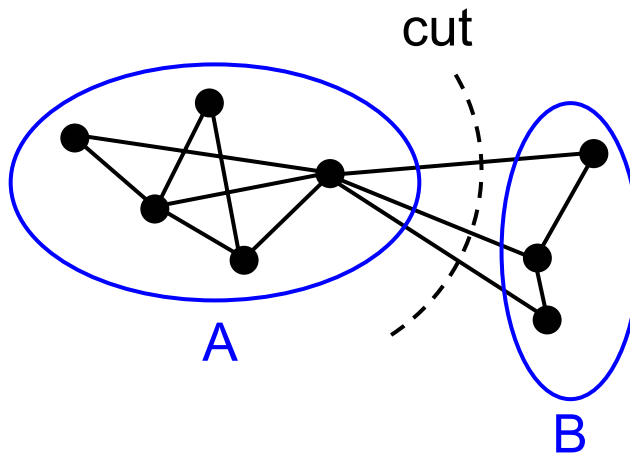
V = vertices  
E = Edges



V = image pixels  
E = pixel similarity

Segmentation = Graph Partitioning

# Min-Cut Segmentation



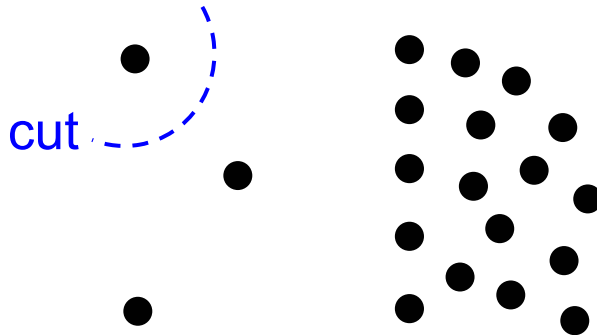
$$\text{cut}(A, B) = \sum_{i \in A, j \in B} W_{ij}$$

Segmentation by min-cut:

Find A, B such that  $\text{cut}(A, B)$  is *minimal*.

(Wu and Leahy 1993)

# Normalized-Cut Segmentation



Min-cut segmentation favors small segments.

Segmentation by normalized-cut:

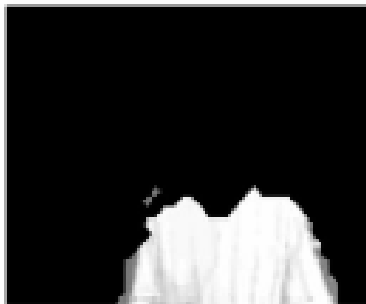
Find A,B such that  $Ncut(A,B)$  is *minimal*.

$$Ncut(A,B) = \sum_{i \in A, j \in B} W_{ij} \left( \frac{1}{\text{vol}(A)} + \frac{1}{\text{vol}(B)} \right)$$

where  $\text{vol}(A) = \sum_{i \in A, j \in A} W_{ij}$

(Shi and Malik 2000)

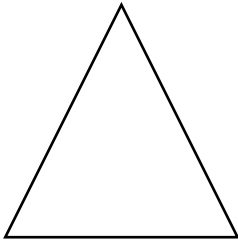
# Normalized-Cut Segmentation - Examples



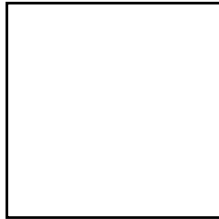
(from Cohen-Or 2005)

# Shape Matching / Object Recognition

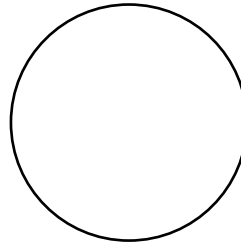
Model #1



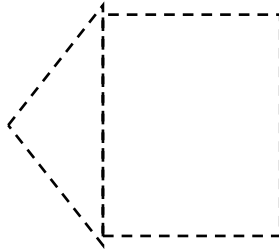
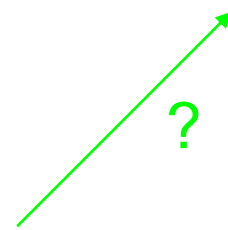
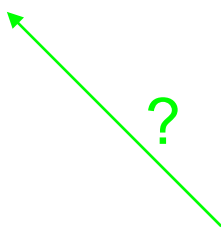
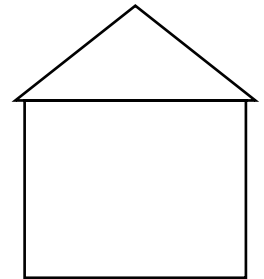
Model #2



Model #3



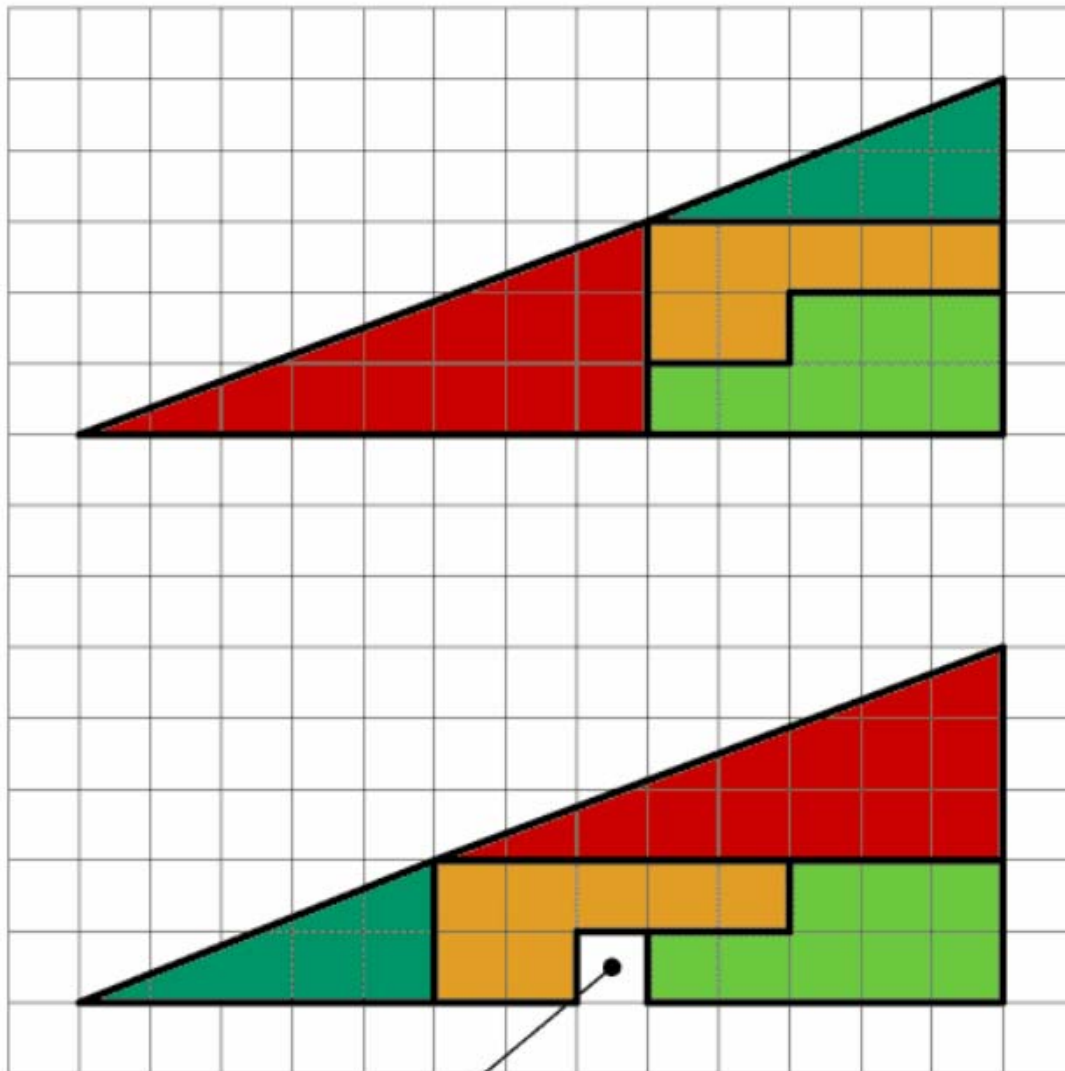
Model #4



## Which Model matches the Measurement?

- Which Model
- What is the transformation from Model to Measurement (translation, rotation, scale,...)

HOW CAN THIS BE TRUE ?



*Below the four parts are moved around*

*The partitions are exactly the same, as those used above*

*From where comes this "hole" ?*